# THE BULLETIN OF SYMBOLIC LOGIC

## EDITED BY

ANDREAS R. BLASS, Managing Editor John P. Burgess Matthew Foreman Akihiro Kanamori Phokion Kolaitis Manuel Lerman H. Dugald Macpherson

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Alasdair Urquhart, Reviews Managing Editor Lev Beklemishev David Evans Erich Grädel Geoffrey Hellman Denis Hirschfeldt Thomas Jech Julia Knight Michael C. Laskowski Volker Peckhaus Wolfram Pohlers Sławomir Solecki

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