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OF  
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EDITED BY

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## ERRATA

### VOLUME 4

Page 124, line 2 from below. Replace the last «R» by «M».

### VOLUME 27

Page 220, line 14 from below. For «FISCHER», read «FISHER».

Page 220, line 14 from below. For «Fischer», read «Fisher».

### VOLUME 30

Page 379, line 17. For «dceide», read «decide».

### VOLUME 32

Page 136, line 6. Insert «no. 12» after «vol. 1».

Page 136, line 12. Insert «no. 10» after «vol. 1».

Page 419, line 12 from below. The first right parenthesis should be replaced by a comma.

### VOLUME 34

Page 106, line 12 from below. «*Über Sinn und Bedeutung*» should be in lightface italic type.

Page 706, column 2, lines 18–21. Entries are in the wrong order, as XXXIV 315 is a review of the first edition XXVII 73 (not of the second edition).

Page 709, column 2, line 24. Discussion is of XXXIII 633, and should be run into the preceding line.

Page 726, column 2, lines 16–14 from below. Entries are in the wrong order, as XXXIV 523 is a review of XXV 381 (not of its German translation).

### VOLUME 35

Page 347, line 22 from below. For «BRACIU», read «VRACIU».

Page 459, lines 28–29. «Societas Scientiarum Fennica, Commentationes physico-mathematicae» should be lightface roman type.

Page 659, line 4. For «XXXV 245(5)», read «XXXV 295(5)».

### VOLUME 36

Page 184, line 10. For «XXXVI 168», read «XXXVI 177».

Page 351, line 22, «*Abriß der Geschichte der Logik*» should be boldface italic type; also for «3537», read «3537».

Page 352, line 14. For «STEINUS», read «STENIUS».

Page 353, line 8 from below. For «p. 54», read «pp. 57–58».

Page 432, line 21. For «MOTO-O-TAKAHASHI», read «MOTO-O TAKAHASHI».

Page 524, line 9 from below. Insert «(1)» after «sequent». Subsequent occurrences of «(1)» refer to this insertion.

Page 550, line 15 from below. For «non-contradition», read «non-contradiction».

Page 553, line 15. For «*Erläuterungen*», read «*Erläuterungen*».

Page 561, line 11. For «Kelson», read «Kelsen».

Page 563, line 12. For «Pierces», read «Peirce».

Page 565, line 14 from below. Insert «(8)» after «XXXIV 151».

Page 571, line 1. For «Z», read «z̄» with acute accent.

Page 571, line 20. For «pp. p–48», read «pp. 9–48».

Page 703, line 2 from below. For «if», read «iff».

Page 758, column 2, lines 12–11 from below. For «BRACIU» read «VRACIU», and for «Braciu» read «Vraciu».

Page 767, column 2, line 8 from below. For «Braciu», read «Vraciu».