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213 Variations on a Theme of Borel

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Variations on a Theme of Borel
An Essay on the Role of the Fundamental
Group in Rigidity

SHMUEL WEINBERGER
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