

THE
JOURNAL
OF
SYMBOLIC LOGIC

EDITED BY

ALONZO CHURCH S. C. KLEENE ALICE A. LAZEROWITZ

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VOLUME 22

1957

PUBLISHED QUARTERLY BY THE ASSOCIATION FOR SYMBOLIC LOGIC, INC.
WITH SUPPORT FROM INSTITUTIONAL MEMBERS

UNIVERSITY OF CHICAGO
DARTMOUTH COLLEGE
DUKE UNIVERSITY
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The four numbers of Volume 22 were issued at the following dates:

Number 1, pages 1–112, August 1, 1957.

Number 2, pages 113–224, October 2, 1957

Number 3, pages 225–336, December 19, 1957

Number 4, pages 337–442, July 1958

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Reprinted 1983

TABLE OF CONTENTS

| | |
|---|-----|
| A generalization of the concept of ω -completeness. By LEON HENKIN | 1 |
| Eulerian syllogistic. By IVO THOMAS | 15 |
| Sur la structuration du tableau des connectifs interpositionnels binaires. By ROBERT BLANCHÉ | 17 |
| A theory of restricted quantification I. By THEODORE HAILPERIN | 19 |
| Two theories with axioms built by means of pleonasms. By ANDRZEJ EHRENFEUCHT | 36 |
| Decidability and essential undecidability. By HILARY PUTNAM | 39 |
| Languages in which self reference is possible. By RAYMOND M. SMULLYAN | 55 |
| Reviews | 68 |
| Twenty-first annual meeting of the Association for Symbolic Logic. By L. GÁL | 105 |
| Abstracts of papers | 105 |
| Elections | 112 |
| A theory of restricted quantification II. By THEODORE HAILPERIN | 113 |
| Uniformization of linear arrays. By N. J. FINE and R. HARROP | 130 |
| On the axioms of order and succession. By KURT BING | 141 |
| The axiomatization of arithmetic. By HAO WANG | 145 |
| A criterion for completeness of degrees of unsolvability. By RICHARD FRIEDBERG | 159 |
| Degrees of unsolvability associated with classes of formalized theories. By SOLOMON FEFERMAN | 161 |
| New foundations for Lewis modal systems. By E. J. LEMMON | 176 |
| On the representation of Herbrand functions in algebraically closed fields. By A. H. LIGHTSTONE and A. ROBINSON | 187 |
| Reviews | 205 |
| Can the logic of indirect discourse be formalised. By L. JONATHAN COHEN | 225 |
| Inference by complementary elimination. By BERNARD K. SYMONDS and RODERICK M. CHISHOLM | 233 |

TABLE OF CONTENTS

| | |
|---|-----|
| Inferential equivalence and natural deduction. By H. HIŻ | 237 |
| Independent axiom schemata for von Wright's <i>M</i> . By ALAN ROSS ANDERSON | 241 |
| Vicious circle principle and the paradoxes. By K. JAAKKO J. HINTIKKA | 245 |
| Linear reasoning. A new form of the Herbrand-Gentzen theorem. By WILLIAM CRAIG | 250 |
| Three uses of the Herbrand-Gentzen theorem in relating model theory and proof theory. By WILLIAM CRAIG | 269 |
| Reviews | 286 |
| Some results in Church's restricted recursive arithmetic. By JOYCE FRIEDMANN | 337 |
| A definition of existence in terms of abstraction and disjunction. By FREDERIC B. FITCH | 343 |
| On logically false evidence statements. By HUGUES LEBLANC | 345 |
| Reviews | 350 |
| List of officers and members of the Association for Symbolic Logic | 410 |
| Index of reviews | 422 |

ERRATA

VOLUME 19

Page 39, line 4. The italic *A* should be roman.

VOLUME 20

Page V. Delete the indicated correction to volume 19, page 38, line 4.

Page 291, line 5. Insert «*against descriptions*» following «*names*».

Page 358, line 9. For «*simplication*», read «*simplification*».

VOLUME 21

Page 79, line 1. Insert «*the*» before «*synthetic*».

Page 82, line 3. For «*an P-description*», read «*a P-description*».

Page 211, line 3 from below. For 265, read 266.

Page 271, last line of footnote. For ϵ , read $\not\epsilon$.

Page 330, line 14 from below. For «*dont'*», read «*don't*».

Page 384, line 11. For «*propositions*», read «*presuppositions*».

Page 389, line 12. For «*vol. 29*», read «*vol. 28*».

Page 399, line 25. For «*1941*», read «*no. 2 (1941)*».

Page 405, line 8. For *Z*, read *S*.

Page 409, line 15. Replace comma at the end of the line by a period.

Page 409, lines 3 and 4 from below. The letter «*a*» should be deleted in each of the four formulas.

Page 411, line 12, displayed formula. Replace the subscript 1 to p by a subscript i .

Page 416, line 4. For «**Bar-Hiliii**», read «**Bar-Hillel**».

VOLUME 22

Page 41, second line of footnote. For «*Harvard*», read «*Holt*».

Page 71, line 3. For «*exsistential*», read «*existential*».

Page 76, line 15. For σ , read σ' .

Page 79, line 24. For «*pp. 112*», read «*112 pp.*».

Page 79, line 19 from below. For «*clod*», read «*closed*».

Page 82, line 14. Insert space after «*only*».

Page 82, line 15. Delete space after ($\exists x$).

Page 99, lines 17 and 18 from below. Read «*Časopis pro pěstování matematiky*, vol. 78 (1953), pp. 373–375».

Page 99, line 12 from below. For «*no. 2*», read «*vol. 2*».

Page 169, footnote 9, line 3. For «*Rassers's*», read *Rosser's*.

ERRATA

Page 205, line 19 from below. For first «of», read «or».

Page 217, line 13. For \mathcal{O} , read \mathcal{Q} .

Page 217, line 25. For «Thorien», read «Theorien».

Page 297, line 27. For «S. 34–67», read «S. 55–67».

Page 300, line 14 from below. For «*Acte*», read «*Actes*».

Page 312, line 20. Insert a left parenthesis before «*Analysis*».

Page 319, line 12 from below. For 1957, read 1956.