

COMPRESSIVE STRENGTH PROPERTIES OF SNOW

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ABSTRACT. The compressive strength of snow cylinders was investigated as a function of the age of the snow from which the cylinders were made, the snow particle size and the age of the cylinders. The results show that the compressive strength is reduced if the snow is older, if the particle size is smaller, or if the cylinders are younger. The variation with age of the cylinders can be represented by an equation similar to that for a first-order chemical reaction. The effect of adding small quantities of various gases to the atmosphere in which the cylinders were kept was also investigated; carbon dioxide and methane had no measurable effect, but ammonia lowered the strength of the cylinders. All the strength measurements were carried out at -10°C .

ZUSAMMENFASSUNG. Es handelt sich um die Untersuchung der Druckfestigkeit von Schneezylindern als Funktion des Alters vom Schnee, aus dem die Zylinder gemacht waren, der Teilchengrösse des Schnees und des Alters der Zylinder. Die Resultate erwiesen, dass bei älterem Schnee, bei kleinerer Teilchengrösse, oder wenn die Zylinder jünger sind, die Druckfestigkeit reduziert wird. Die Schwankung mit dem Alter der Zylinder lässt sich durch eine Gleichung ähnlich der Gleichung einer chemischen Reaktion erster Ordnung wiedergeben. Ausserdem wurde untersucht, wie sich der Zusatz kleiner Mengen verschiedener Gase zur Atmosphäre, in der die Zylinder gehalten wurden, auswirkte; Kohlensäure und Methan hatten keine messbare Wirkung, aber Ammoniak reduzierte die Festigkeit der Zylinder. Alle Festigkeitsmessungen wurden bei einer Temperatur von -10°C ausgeführt.

INTRODUCTION

Extensive studies of the strength properties of snow were made by Butkovich,¹ who investigated the compressive, tensile, shear and torsional strengths of snow as a function of density. A very pronounced dependence of the strength on the density was found which could be expressed in a general formula. The work of disaggregation as a function of density was also reported by Butkovich, who also gives relevant literature references. Bender² has also studied the age hardening of snow by measuring the work of disaggregation. In the present work a beginning has been made of a study of the uniaxial compressive strength of snow cylinders as a function of age and of particle size of snow fractions. Ageing of snow and the effect on the compressive strength of snow of the inclusion of various gases in the atmosphere in which they were kept, were also investigated.

EXPERIMENTAL DETAILS

Materials. Two different snows were used for the experiments. One snow was collected at Wilmette, and stored at -20°C .; experiments were started after about two weeks; the other was collected at Houghton, Michigan, stored at about -15°C . for about four weeks prior to use and subsequently stored at -20°C .

Preparation of Snow Fractions. The snow fractions were prepared on a "Ro-Tap" shaker; the sieves used were of the U.S. standard sieve series. The snow for each of the Houghton snow fractions was obtained after two minutes shaking, whereas the Wilmette snow fractions were obtained after longer periods of shaking, especially for the small size and largest size of particles.

Apparatus and Technique. All strength measurements were carried out at $-10^{\circ}\pm 0.5^{\circ}\text{C}$. with a Carver Hydraulic Laboratory Press in conjunction with a Baldwin Load Cell (2000 lb., 900 kg.) and a Leeds and Northrup recorder. A picture of this press is shown in a report by Butkovich on the Ultimate Strength of Ice.³

The snow cylinders were prepared at -20°C . in a Lucite cylinder of 4.38 cm. inside diameter and 25 cm. high. The height was graduated and could easily be read to the nearest mm. About 82.5 gm. of snow were weighed into the tube with an accuracy of 0.1 gm. The snow was then compressed to a height of 10 cm. in the plastic tube with the press to which a

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suitable piston was attached. Actually only half the compression was carried out at a time, the cylinder was then inverted and the compression completed. Thus large density gradients in the cylinders were avoided. The majority of densities were in the range from 0.548 to 0.552 gm./cm.³. The snow cylinders (diameter 4.38 cm., height 10 cm.) were then removed to a cold room of -10° C. and crushed after a time interval as indicated in the experimental results.

EXPERIMENTAL RESULTS

Ageing of Snow Cylinders. The ageing of snow cylinders was investigated using the unfractionated, original snow samples, except that the Houghton snow was passed through a 1.19 mm. sieve to remove lumps. Tables I and II and Figs. 1 and 2 show the experimental results for the Wilmette snow. Table III and Fig. 3 show the results for the Houghton snow.

TABLE I. COMPRESSIVE STRENGTH AS A FUNCTION OF AGEING OF SNOW CYLINDERS AT -10° C.
Wilmette Snow unfractionated
Age of snow: 35-50 days

Age of snow days	Age of cylinders hours	Mean compressive strength kg./cm. ²	Standard deviation kg./cm. ²	Standard error of mean kg./cm. ²
43	c. 0.1	2.9	±0.6	±0.2
45	7.1	4.7	±1.1	±0.3
50	22.7	6.8	±1.2	±0.4
35	28.7	10.6	±2.0	±0.6
42	69.0	9.6	±1.5	±0.4
45	92.4	10.9	±2.5	±0.7
37	117.9	13.5	±1.4	±0.4
36	167.3	15.9	±1.7	±0.5
43	212.5	11.0	±1.4	±0.4

TABLE II. COMPRESSIVE STRENGTH AS A FUNCTION OF AGEING OF SNOW CYLINDERS AT -10° C.
Wilmette snow unfractionated
Age of snow: 57 days

Age of cylinders hours	Mean compressive strength kg./cm. ²	Standard deviation kg./cm. ²	Standard error of mean kg./cm. ²
0.05	1.6	±0.5	±0.1
4.6	3.6	±0.8	±0.2
23.7	7.1	±1.6	±0.5
29.14	7.7	±1.3	±0.4
45.5	8.0	±0.9	±0.3
96.1	8.8	±1.3	±0.4
139.5	7.5	±1.1	±0.3
186.4	9.0	±1.5	±0.4

TABLE III. COMPRESSIVE STRENGTH AS A FUNCTION OF AGEING OF SNOW CYLINDERS AT -10° C.
Houghton snow
Age of snow: 30 days

Age of cylinders hours	Mean compressive strength kg./cm. ²	Standard deviation kg./cm. ²	Standard error of mean kg./cm. ²
0.02	1.5	±0.9	±0.3
5.9	3.9	±0.7	±0.2
21.7	5.1	±1.4	±0.4
45.7	8.5	±1.5	±0.5
71.9	8.3	±1.1	±0.3
119.9	9.9	±1.2	±0.4
166.7	10.6	±2.7	±0.9

The cylinders fractured usually into three pieces in a similar way to that observed by Butkovich (see Fig. 1 of Butkovich's report¹). The number near each of the experimental points in Fig. 1 gives the age of the snow in days from which the twelve cylinders, whose mean strength the points represent, were made. It is seen that the younger the snow, the greater the strength of the cylinders. The cylinders from the Wilmette snow represented in

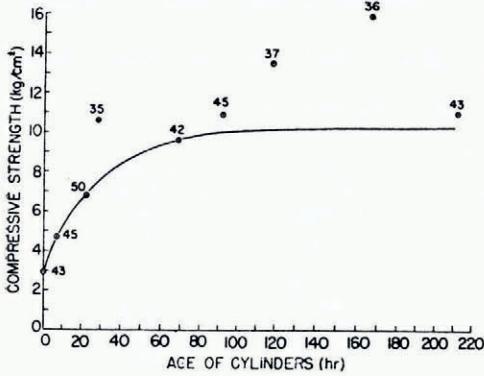


Fig. 1

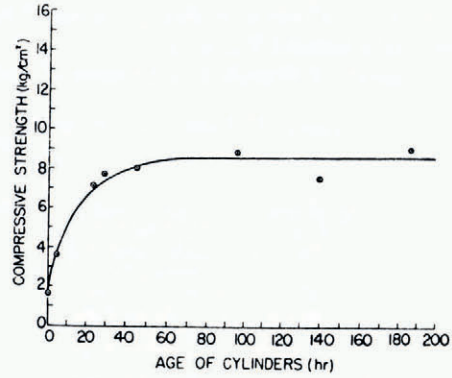


Fig. 2

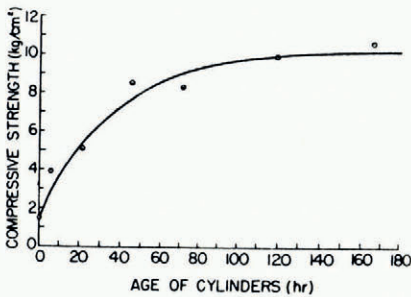


Fig. 3

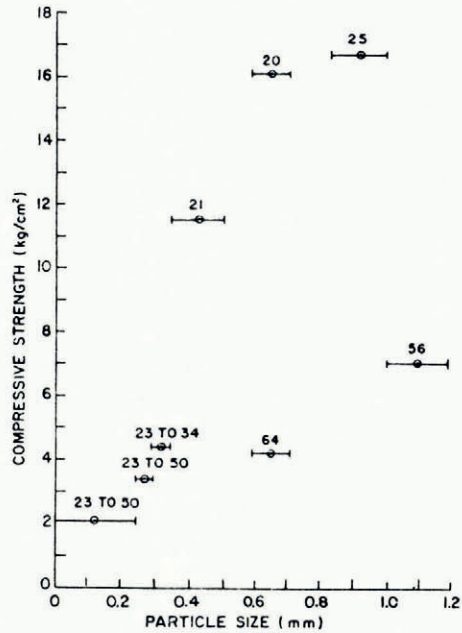


Fig. 4

Fig. 1. Compressive strength of snow cylinders (radius 2.19 cm., height 10 cm., density c. 0.550 gm./cm.³) as a function of the age of the cylinders at -10° C. Each point represents the average of twelve tests. The numbers near the points represent the age in days of the snow from which the cylinder was made. Snow was collected at Wilmette, Illinois. Curve was calculated from equation (1a) with the following constants:

$$S_0 = 2.8 \text{ kg./cm.}^2, S_f = 10.3 \text{ kg./cm.}^2, k = 3.52 \times 10^{-2} \text{ hr.}^{-1}$$

Fig. 2. Compressive strength of snow cylinders (radius 2.19 cm., height 10 cm., density c. 0.550 gm./cm.³) as a function of the age of the cylinders at 10° C. Each point represents the average of twelve tests. The age of the snow when preparing cylinders was in all cases 57 days. Snow was the same (Wilmette) as that for Fig. 1. Curve was calculated from equation (1a) with the following constants:

$$S_0 = 1.5 \text{ kg./cm.}^2, S_f = 8.6 \text{ kg./cm.}^2, k = 6.45 \times 10^{-2} \text{ hr.}^{-1}$$

Fig. 3. Compressive strength of snow cylinders (radius 2.19 cm., height 10 cm., density c. 0.550 gm./cm.³) as a function of the age of the cylinders at -10° C. Each point represents the average of ten tests. The age of the snow when preparing cylinders was in all cases 28 days. Snow was collected at Houghton, Michigan. Curve was calculated from equation (1a) with the following constants:

$$S_0 = 1.5 \text{ kg./cm.}^2, S_f = 10.3 \text{ kg./cm.}^2, k = 2.70 \times 10^{-2} \text{ hr.}^{-1}$$

Fig. 4. Compressive strength of snow cylinders as a function of snow particle size (-10° C.). The horizontal lines represent the range of sieve sizes used to obtain the particular fraction. Each point represents the average of twelve tests. The number beside each point gives the age of the snow (Wilmette snow). Each cylinder was aged for 168 hr. at -10° C.

Fig. 2 were all made within 30 hours of each other, as were the cylinders from the Houghton snow represented in Fig. 3.

Compressive Strength as a Function of Particle Size. Table IV gives the compressive strength

TABLE IV. COMPRESSIVE STRENGTH AS A FUNCTION OF PARTICLE SIZE AT -10° C.
Wilmette snow
Age of cylinders: 168 hours

Age of snow days	Sieve range mm.	Mean compressive strength kg./cm. ²	Standard deviation kg./cm. ²	Standard error of mean kg./cm. ²
22	Unfractionated original snow	19.7	± 4.2	± 1.2
56	1.19-1.00	7.0	± 1.9	± 0.9
25	1.00-0.840	16.7	± 3.3	± 0.9
20	0.710-0.590	16.1	± 2.1	± 0.6
64	0.710-0.590	4.2	± 1.2	± 0.6
21	0.500-0.350	11.5	± 2.8	± 0.8
23 to 34	0.350-0.297	4.4	± 1.7	± 0.5
23 to 50	0.297-0.250	3.4	± 2.3	± 0.7
23 to 50	0.250-0.000	2.1	± 1.3	± 0.5

values as a function of particle size, and Fig. 4 shows the mean strength values as a function of particle size for the Wilmette snow. Most of the Wilmette snow (*c.* 50 per cent.) was in the size range from 3.5 to 5.0 mm. There is a very appreciable decrease of strength with particle size. Fig. 4 shows again the marked influence of the age of the snow. It was desired at a later date to determine the strength of the snow fraction of large particle size. These later strength values for the older snow were very much lower (see Table IV and Fig. 4, 56 days) than expected from the previous results. In order to check this behavior, tests were repeated on a snow fraction which had been investigated about six weeks earlier. This means that cylinders were prepared of snow six weeks older than that used for the previous fraction. The results (Table IV and Fig. 4, 64 days) show that the strength of the cylinders is very dependent on the age of the snow. This strong dependence is also apparent for the three fractions of small particle size. These measurements were made before the importance of age was realized. For this reason the average strength values for the smaller size fractions are considered to be too small compared with those of the larger size fractions of Table IV.

An interesting by-product of this work is given by the densities of the snow fractions before compacting. These densities were obtained by pouring the fractions loosely into the plastic cylinder without compacting. Fig. 5 shows the results. A decrease of density with increasing particle size is observed.

Because of the strong influence of the age of snow on its strength, a series of experiments were carried out with the Houghton snow on the strength as a function of particle size, all cylinders being prepared within 30 hours of each other.

These results are shown in Table V and Fig. 6. Here again the compressive strength

TABLE V. COMPRESSIVE STRENGTH AS A FUNCTION OF PARTICLE SIZE AT -10° C.
Houghton snow
Age of snow: 27 to 28 days
Age of cylinders: 168 hours

Sieve range mm.	Mean compressive strength kg./cm. ²	Standard deviation kg./cm. ²	Standard error of mean kg./cm. ²
Original, unfractionated snow	10.6	± 2.7	± 0.9
1.00-0.840	8.0	± 2.0	± 0.6
0.840-0.710	9.0	± 0.8	± 0.3
0.710-0.590	6.7	± 1.2	± 0.4
0.590-0.500	4.9	± 1.3	± 0.4
0.500-0.350	4.7	± 1.1	± 0.5
0.350-0.250	4.1	± 1.1	± 0.3
0.250-0.074	4.2	Too few samples	

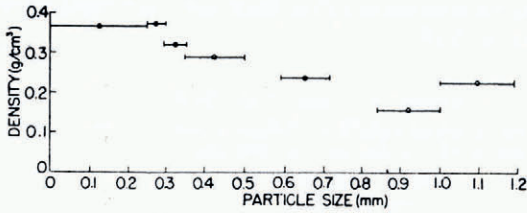
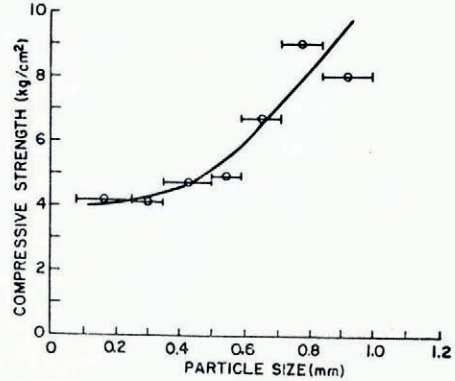


Fig. 5 (left). Density obtained by loosely packing snow fractions (-20°C). (Wilmette snow)

Fig. 6 (right). Compressive strength of snow cylinders as a function of snow particle size (-10°C). The horizontal lines represent the range of sieve sizes used. Each point represents the mean of ten tests. Age of snow in all cases was 28 days (Houghton snow). Each cylinder was aged for 168 hr. before breaking



decreases with particle size, however not quite as drastically as for the Wilmette snow. The difference is due to the high age of the lower Wilmette fractions as pointed out previously.

Mixture of Fractions. A number of experiments were also carried out on the strength of mixtures of fractions of the Wilmette Snow. On the whole these results reflect those which were found with single fractions. The results are given in Table VI.

TABLE VI. COMPRESSIVE STRENGTH OF MIXTURES OF FRACTIONS AT -10°C .

Composition of fraction	Wilmette snow		
	Mean compressive strength kg./cm. ²	Standard deviation kg./cm. ²	Standard error of mean kg./cm. ²
Fraction 1.00 mm.-0.840 mm. plus fraction 0.710 mm.-0.590 mm. plus fraction 0.500 mm.-0.350 mm. 1 : 1 : 1 by weight. Age of snow 71 days	5.4	± 1.9	± 0.5
Fraction 0.710 mm.-0.590 mm. plus fraction 0.500 mm.-0.350 mm. plus fraction 0.350 mm.-0.297 mm. 1 : 1 : 1 by weight. Age of snow 63 days	3.4	± 0.8	± 0.2
Fraction 0.500 mm.-0.350 mm. plus fraction 0.350 mm.-0.297 mm. plus 0.250 mm.-0 mm. 1 : 1 : 1 by weight. Age of snow 66 days	1.05	± 0.6	± 0.2
3 parts of weight of fraction 1.00 mm. to 0.71 mm. plus 1 part of fraction 0.35 mm. to 0 mm. Age of snow 79 days	3.2	± 1.1	± 0.3
19 parts by weight of fraction 0.840 mm. to 0.710 mm. plus 1 part of fraction 0.074 mm. to 0 mm. Age of snow 89 days	2.7	—	—
Fraction 0.840 mm to 0.710 mm. alone ..	2.7	—	—

INFLUENCE OF GASES ON THE COMPRESSIVE STRENGTH OF SNOW

A number of snow cylinders were prepared which were exposed to gases such as carbon dioxide (CO₂), methane (CH₄) and ammonia (NH₃). Other cylinders were prepared at the

same time for comparison and treated in the same way except that they were not exposed to the gases. These are referred to as blanks in Table VII.

TABLE VII. EFFECT OF GASES ON THE COMPRESSIVE STRENGTH OF SNOW

(a) Original Wilmette Snow treated with NH₃ before making cylinders. Cylinders aged for 168 hours at -10° C. before breaking. No evacuation. Samples smelled of NH₃ at the time of breaking.

Density g./cm. ³	Compressive strength kg./cm. ²	Work of compression from 13 cm. to 10 cm. height kg. cm.	Remarks
0.549	25.1	140	Blank
0.550	16.9	76	Blank
0.551	10.6	75	Treated
0.553	9.1	58	Treated

(b) Original Wilmette Snow. Cylinders treated with NH₃. Cylinders stood in the open for 3 hours at -20° C. Scarcely a smell of NH₃ left. Then aged for 168 hours at -10° C. before breaking.

Density g./cm. ³	Compressive strength kg./cm. ²	Remarks
0.547	8.2	Blank
0.553	15.1	Blank
0.550	11.5	Blank
0.553	14.5	Blank
0.547	10.9	Blank
0.549	10.6	Blank
Mean	11.8	
Standard deviation	±2.6	
Standard error of mean	±1.1	
0.549	8.8	Treated
0.549	8.8	Treated
0.549	4.5	Treated
0.550	9.4	Treated
0.548	6.7	Treated
0.549	7.6	Treated
Mean	7.6	
Standard deviation	±1.8	
Standard error of mean	±0.8	

(c) Original Wilmette Snow. Evacuated for 1½ hours at -10° C. after NH₃ treatment. Cylinders aged 168 and 336 hours, respectively.

Density g./cm. ³	Compressive strength kg./cm. ²	Remarks
0.549	18.4	Blank, aged 168 hours
0.549	17.2	" " "
0.550	17.8	" " "
Mean	17.8	
0.551	10.9	Treated, aged 168 hours
0.549	10.6	" " "
0.550	11.8	" " "
Mean	11.1	
0.549	16.9	Blank, aged 336 hours
0.549	16.9	" " "
0.551	19.4	" " "
Mean	17.7	
0.549	10.6	Treated, aged 336 hours
0.549	10.9	" " "
Mean	10.8	

(d) Original Wilmette Snow. Cylinders after NH₃ treatment were compressed in Lucite tubes from 10 cm. to 9 cm. height and then cut to 8 cm. height. Evacuated as before and aged for 168 hours at -10° C.

Density g./cm. ³		Compressive strength kg./cm. ²	Compressive work from 10 to 9 cm. height kg. cm.	Remarks
at 10 cm.	at 9 cm.			
0.551	0.607	34.8	460	Blank
0.550	0.606	39.8	420	"
0.551	0.607	24.0	400	"
0.549	0.604	41.3	440	"
0.551	0.606	42.8	415	"
0.549	0.605	34.2	420	"
Mean		36.2	426	
Standard deviation		±6.9		
Standard error of mean		±2.9		
0.552	0.608	11.7	300	Treated
0.553	0.609	23.7	280	"
0.552	0.608	18.6	325	"
0.549	0.605	19.2	280	"
0.551	0.607	17.4	315	"
0.550	0.606	13.2	280	"
Mean		17.3	297	
Standard deviation		±4.3		
Standard error of mean		±1.8		

(e) Original Wilmette Snow. Cylinders treated with CO₂, evacuated and then aged for 168 hours at -10° C.

Density g./cm. ³	Compressive strength kg./cm. ²	Remarks
0.548	11.5	Blank
0.550	12.1	"
0.552	11.5	"
0.551	13.0	"
0.551	10.3	"
0.550	13.6	"
Mean	12.0	
Standard deviation	±1.2	
Standard error of mean	±0.5	
0.548	13.9	Treated
0.551	14.5	"
0.551	10.6	"
0.549	11.2	"
0.551	9.4	"
0.551	11.2	"
Mean	11.8	
Standard deviation	±2.0	
Standard error of mean	±0.8	

(f) Original Wilmette Snow. Cylinders treated with CH₄, evacuated and then aged for 168 hours at -10° C.

Density g./cm. ³	Compressive strength kg./cm. ²	Remarks
0.551	12.1	Blank
0.548	10.3	"
0.552	10.9	"
Mean	11.1	
0.552	10.3	Treated
0.550	11.2	"
0.552	10.3	"
Mean	10.6	

The experimental procedure was as follows. The cylinders were made in the usual way at -20° C. They were then placed in a wide-necked bottle and exposed to a small amount of gas. The amounts were measured approximately by counting bubbles passed through a washbottle (160 bubbles for each experiment, or very approximately 100 to 150 ml. at N.T.P.). The samples treated with carbon dioxide and methane did not show any difference from the untreated samples, whereas the samples treated with ammonia had a distinctly wet appearance. The untreated and treated samples were then evacuated under a bell jar until the ammonia smell could not be detected any more; the samples treated with the other two gases were evacuated for the same length of time. The cylinders were then stored for 168 hours at -10° C. and broken. The results are given in Table VII. It is seen that the strength of the cylinders treated with ammonia has decreased considerably compared with untreated samples, whereas carbon dioxide and methane apparently do not influence the strength.

DISCUSSION

The ageing curves for the snow cylinders made from the Wilmette and Houghton snows can be fitted very satisfactorily by an equation as follows:

$$\frac{S_f - S_t}{S_f - S_0} = \exp(-kt), \quad (1a)$$

or

$$\ln \frac{S_f - S_0}{S_f - S_t} = kt, \quad (1b)$$

where S_0 is the initial and S_f the final compressive strength and k a rate constant. The curves in Figs. 1, 2 and 3 were calculated with the following constants:

Wilmette Snow (Fig. 1) $S_0 = 2.8 \text{ kg./cm.}^2$, $S_f = 10.3 \text{ kg./cm.}^2$,
 $k = 3.52 \times 10^{-2} \text{ hr.}^{-1}$.

Wilmette Snow (Fig. 2) $S_0 = 1.5 \text{ kg./cm.}^2$, $S_f = 8.6 \text{ kg./cm.}^2$,
 $k = 6.45 \times 10^{-2} \text{ hr.}^{-1}$.

Houghton Snow (Fig. 3) $S_0 = 1.5 \text{ kg./cm.}^2$, $S_f = 10.3 \text{ kg./cm.}^2$,
 $k = 2.70 \times 10^{-2} \text{ hr.}^{-1}$.

It should be noted that equation (1a) and (1b) is the same as that for a first-order chemical reaction where one compound B is formed from a compound A: $A \rightarrow B$. Differentiation of (1a) gives:

$$dS_t/dt = k(S_f - S_t), \quad (2)$$

and at $t = 0$, $S_t = S_0$.

Some experiments performed by Bender² on the work of disaggregation are shown in Fig. 7. These results can also be expressed by equation (1a), although not quite as closely as the previous ones. It would be of interest to study the ageing of snow as a function of temperature. The rate constant k can probably be expressed by an exponential law, $k = A \exp(-E/RT)$, where A and E are constants, R the gas constant, and T the absolute temperature. An energy of activation E could then be derived, which might throw some light on the ageing process. This ageing process has something to do with recrystallization, diffusion and sublimation in the contact areas between snow particles.

The great effect of the age of the snow from which they are made on the compressive strength of the cylinders of equal age is quite remarkable. This must be due to the metamorphism⁴ snow undergoes as it ages. New snow particles have numerous ramifications and protuberances, which are in an unstable state. Recrystallization, sublimation and surface migration take place rounding the particles. Thus the whole system tends to become more stable with age. Consequently, less bonding will take place on compression with old than with

new snow. The strength of snow specimens as a function of the age of snow merits further study.

The decrease of compressive strength with decrease in particle size seems surprising at first. Microscopic examination shows that the snow passes from a more spherical shape to a more elongated one as the particle size decreases. It seems also to be the case that the smaller particles have less ramifications than the larger ones. One factor which might be of decisive importance in this connexion is the following. It was shown in Fig. 6 that the smaller the particle size, the higher the density obtained by just pouring the sample into the plastic cylinder. Probably less work of compaction is required to compress the finer particles to the same density than the larger ones. Therefore the larger particles will be under much more

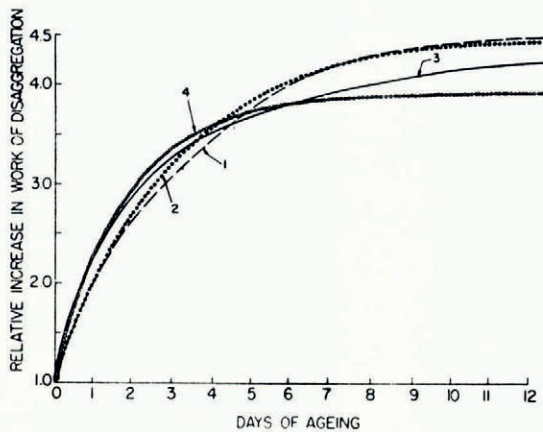


Fig. 7. Ratio of work of disaggregation at time t to work at $t = 0$ as a function of time. Curves (1) and (2) are averaged experimental curves for -5°C . and -20°C . respectively. Curves (3) and (4) are calculated from equation (1a).

Curve (3): $S_0 = 1\text{ kg./cm.}^2$, $S_f = 3.9\text{ kg./cm.}^2$, $k = 5.61 \times 10^{-1}\text{ day}^{-1}$.

Curve (4): $S_0 = 1\text{ kg./cm.}^2$, $S_f = 4.5\text{ kg./cm.}^2$, $k = 3.31 \times 10^{-1}\text{ day}^{-1}$. Experimental results were obtained by Bender.³

strain and stress than the smaller ones. In order to relieve this unstable condition, re-arrangement has to take place, which leads to finer bonding. It would be of interest to carry out studies on fractions of differently shaped snow particles, such as spheres, needles, etc. A beginning has been made by Fuchs.⁵ It would also be of interest to study snow cylinders by the replica technique developed by Fuchs.⁶ This would give an insight as to the number of bridges between snow particles as a function of specimen density, temperature, work of compression, etc.

The effect of gases, such as ammonia (NH_3) is not surprising. An exothermic reaction takes place forming NH_4OH . A concentrated solution is produced on the surface of the particles which serves as a lubricant for further compression. However, it does not seem possible to remove subsequently all of the NH_4OH and $(\text{NH}_4)_2\text{CO}_3$ which is formed by absorption of CO_2 from the air. Thus a film will be left between the snow particles weakening the whole structure. Experiments also show that for the same work of compression, the untreated snow still has a higher strength.

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