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EDITED BY

ALONZO CHURCH    S. C. KLEENE    ALICE A. LAZEROWITZ

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## ERRATA

### VOLUME 19

Page 39, line 4. The italic *A* should be roman.

### VOLUME 20

Page V. Delete the indicated correction to volume 19, page 38, line 4.

Page 291, line 5. Insert «*against descriptions*» following «*names*».

Page 358, line 9. For «*simplication*», read «*simplification*».

### VOLUME 21

Page 79, line 1. Insert «*the*» before «*synthetic*».

Page 82, line 3. For «*an P-description*», read «*a P-description*».

Page 211, line 3 from below. For 265, read 266.

Page 271, last line of footnote. For  $\epsilon$ , read  $\not\epsilon$ .

Page 330, line 14 from below. For «*dont'*», read «*don't*».

Page 384, line 11. For «*propositions*», read «*presuppositions*».

Page 389, line 12. For «*vol. 29*», read «*vol. 28*».

Page 399, line 25. For «*1941*», read «*no. 2 (1941)*».

Page 405, line 8. For *Z*, read *S*.

Page 409, line 15. Replace comma at the end of the line by a period.

Page 409, lines 3 and 4 from below. The letter «*a*» should be deleted in each of the four formulas.

Page 411, line 12, displayed formula. Replace the subscript 1 to  $p$  by a subscript  $i$ .

Page 416, line 4. For «**Bar-Hiliii**», read «**Bar-Hillel**».

### VOLUME 22

Page 41, second line of footnote. For «*Harvard*», read «*Holt*».

Page 71, line 3. For «*exsistential*», read «*existential*».

Page 76, line 15. For  $\sigma$ , read  $\sigma'$ .

Page 79, line 24. For «*pp. 112*», read «*112 pp.*».

Page 79, line 19 from below. For «*clod*», read «*closed*».

Page 82, line 14. Insert space after «*only*».

Page 82, line 15. Delete space after ( $\exists x$ ).

Page 99, lines 17 and 18 from below. Read «*Časopis pro pěstování matematiky*, vol. 78 (1953), pp. 373–375».

Page 99, line 12 from below. For «*no. 2*», read «*vol. 2*».

Page 169, footnote 9, line 3. For «*Rassers's*», read *Rosser's*.

## ERRATA

Page 205, line 19 from below. For first «of», read «or».

Page 217, line 13. For  $\mathcal{O}$ , read  $\mathcal{Q}$ .

Page 217, line 25. For «Thorien», read «Theorien».

Page 297, line 27. For «S. 34–67», read «S. 55–67».

Page 300, line 14 from below. For «Acte», read «Actes».

Page 312, line 20. Insert a left parenthesis before «Analysis».

Page 319, line 12 from below. For 1957, read 1956.