



# Corrigendum to “Chen Inequalities for Submanifolds of Real Space Forms with a Semi-symmetric Non-metric Connection”

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*Abstract.* We correct the coefficients in inequality (4.1) in Theorem 4.1(i), from C. Özgür and A. Mihai, *Chen inequalities for submanifolds of real space forms with a semi-symmetric non-metric connection*. Canad. Math. Bull. 55(2012), no. 3, 611–622.

## Corrigendum

Due to a minor error of computation (in the expression of the sectional curvature  $K_{ij}$  one term was missed) in the proof of [1, Theorem 4.1], some coefficients in (4.1) should be simplified.

The corrected statement follows.

**Theorem 4.1** Let  $M^n$ ,  $n \geq 3$ , be an  $n$ -dimensional submanifold of an  $(n + p)$ -dimensional real space form  $N^{n+p}(c)$  of constant sectional curvature  $c$  endowed with a semi-symmetric non-metric connection  $\tilde{\nabla}$ .

(i) For each unit vector  $X$  in  $T_x M$  we have

$$\|H\|^2 \geq \frac{4}{n^2} [\text{Ric}(X) - (n-1)(c - \Omega)].$$

(ii) If  $H(x) = 0$ , then a unit tangent vector field  $X$  at  $x$  satisfies the equality case of (4.1) if and only if  $X \in N(x)$ .

(iii) The equality case of (i) holds identically for all unit tangent vectors at  $x$  if and only if either  $x$  is a totally geodesic point, or  $n = 2$  and  $x$  is a totally umbilical point.

**Remark** Relation (4.1) from [1] was

$$(4.1) \quad \|H\|^2 \geq \frac{4}{n^2} \left[ \text{Ric}(X) - (n-1)c + \frac{n-1}{2} \lambda - \frac{(n-2)(n-1)}{2} s(X, X) + \frac{1}{2} (n^2 - n) \phi(H) \right].$$

These new coefficients do not affect items (ii) and (iii) of [1, Theorem 4.1].

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**Remark** In general, for a submanifold  $M^n$  of a real space form endowed with a semi-symmetric non-metric connection, the sectional curvature  $K(\pi)$  of a plane section  $\pi$  (and consequently the Chen invariants) cannot be defined, because it depends of the choice of the orthonormal basis of  $\pi$ . For this reason, we put the condition that  $\Omega(X)$  is constant for all unit vectors tangent to  $M^n$  in [1].

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## References

- [1] C. Özgür and A. Mihai, *Chen inequalities for submanifolds of real space forms with a semi-symmetric non-metric connection*. *Canad. Math. Bull.* 55(2012), no. 3, 611–622.  
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