

# THE JOURNAL OF SYMBOLIC LOGIC

## **Edited by**

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The JOURNAL invites submission of original scholarly work in mathematical logic and its applications.

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