

Advances in Applied Probability

The Editorial Board would like to encourage the submission to the *Advances* of Review Papers summarising and coordinating recent results in any of the fields of Applied Probability. The papers should be approximately 40–50 printed pages in length. On acceptance of a Review Paper for publication in the *Advances*, the author will receive £stg. 100 (U.S. \$240).

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| J. Keilson and S. Subba Rao | A process with chain dependent growth rate — Part II: The ruin and ergodic problems |
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Printed in Israel at the Jerusalem Academic Press, P.O.B. 2390, Jerusalem.

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