On-shell approach to three-body scattering

Andris Talis Stelbovics

Although calculations of low energy elastic neutron-deuteron scattering based on on-shell dispersion relations have met with some success, it is difficult to assess their reliability because of the number of theoretical approximations and experimental uncertainties. In this thesis a study is made of the on-shell approach in the context of the Amado model of neutron-deuteron scattering where comparison with accurate numerical solutions of the off-shell Faddeev equations is possible.

The motivation for the work is discussed in Chapter 1 and the off-shell equations for the models are introduced in Chapter 2. In Chapter 3 the on-shell amplitudes for elastic, breakup and free scattering are constructed as Fredholm series solutions, whose convergence in the limit of physical energies is determined in each case by investigating their analytic structure. As a result we are able to rigorously justify the rotation of contours method used to solve the off-shell equations.

In Chapter 4 the elastic neutron-deuteron scattering amplitudes are continued to complex energies. It is shown that they are analytic on the entire physical sheet with the exception of the real axis along which the singularities are divided into two classes; the left hand potential cuts and right hand unitarity cuts. The special class of pinch singularities between energy denominators is studied and it is found that only a single pinch singularity is possible. Contained in the first iterated term of the multiparticle scattering series it contributes only to the left hand cut.

The methods developed for the elastic amplitudes are extended in Chapter 5 to obtain the analytic structure of the breakup and free scattering amplitudes.

477

   In Chapter 6 a rigorous dispersion relation formulated for the elastic
neutron-deuteron amplitude is solved in the s-wave quartet and doublet
channels using various driving terms generated by the multiple scattering
solution of the Amado model equations. To take account of the breakup
channel exact model inelasticities computed from the off-shell equations
are used. The numerical results indicate that the quartet channel
scattering is well described with the simplest driving terms, but in the
doublet channel the N/D solutions approach the exact model values only
slowly as the order of the inputs is increased. The effect on the
solutions of various approximations to the exact inelasticities is also
tested. The results show that it is important to have a good description
of inelastic effects in both the quartet and doublet channels. From the
calculations it appears that although on-shell techniques are capable of
reproducing the main features of the exact amplitudes they cannot compete
in accuracy with the complete solutions of the off-shell Faddeev equations.

   Chapter 7 is devoted to a numerical study of the eigenvalue spectra of
the kernels of the off-shell equations and a description of the low energy
behaviour of the phase shift in the s-wave doublet in terms of the
eigenvalues is presented.