

THE  
BULLETIN  
OF  
SYMBOLIC LOGIC

EDITED BY

ANDREAS R. BLASS, Managing Editor

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*Articles* should be expository or survey papers of broad interest that are accessible to a wide audience of logicians. They may deal with any areas of logic including mathematical or philosophical logic, logic in computer science or linguistics, the history or philosophy of logic, and applications of logic to other fields.

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