The thermodynamic predictability of sea ice[*]

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ABSTRACT. Statistical analyses and model experiments suggest that the sea-ice cover is predictable weeks to months in advance. As such, it is one of the most highly predictable components of the climate system. The thermodynamic mechanisms by which this predictability can be realized are examined. It is found that the predictability is dependent on the differential growth/decay of sea ice as a function of thickness. In winter or year-round, for thin ice, the growth/decay rates are a strong function of thickness, which gives a relatively short period of predictability, though still long compared to the atmosphere. In summer, or year-round for thick ice, growth/decay rates are only weak functions of thickness and the period of predictability is comparatively long.

1. PHYSICAL PARAMETERS AND THEIR VALUES

f	$m\,s^{-1}$	Ice growth/melt rate
g	m^{-1}	Fraction of area centered at location x,y at time t which is covered by ice of thickness h to $h + \mathrm{d}h$
ρ_a	$1.2\,kg\,m^{-3}$	Air density
U_a	$5\,m\,s^{-1}$	Air speed
C_h	1.75×10^{-3}	Sensible-heat transfer coefficient (Maykut, 1978)
C_p	$1004\,J\,kg^{-1}\,K^{-1}$	Specific heat of air
T_s	K	Surface temperature of ice/snow
T_a		Air temperature
	$243\,K$	Winter
	$278\,K$	Summer
T_f	$271.3\,K$	Freezing point of sea water
C_q	1.75×10^{-3}	Latent-heat transfer coefficient
L_v	$2.834 \times 10^{6}\,J\,kg^{-1}$	Latent heat of vaporization of ice
k_s	$0.31\,W\,m^{-1}\,K^{-1}$	Thermal conductivity of snow
k_i	$2.2\,W\,m^{-1}\,K^{-1}$	Thermal conductivity of ice
H_s	m	Snow thickness
H_i	m	Ice thickness
C		Cloudiness
	0.5	Winter (Parkinson and Washington, 1979)
	0.75	Summer (Parkinson and Washington, 1979)
ϵ_i	0.97	Longwave emissivity of ice (Parkinson and Washington, 1979)

σ	$5.67 \times 10^{-8}\,W\,m^{-2}\,K^{-4}$	Stefan–Boltzmann constant
α		Albedo
	0.8	Winter
	0.5	Summer
LW	$W\,m^{-2}$	Longwave radiation
$SW\downarrow$		Down-welling shortwave-radiation flux
	$0\,W\,m^{-2}$	Winter
	$300\,W\,m^{-2}$	Summer
I_0	0.34	Fraction of shortwave radiation which is not reflected that penetrates the ice surface (Maykut and Untersteiner, 1971)
τ_s	$15\,m^{-1}$	Extinction coefficient for snow after Grenfell and Maykut (1977)
τ_i	$1.5\,m^{-1}$	Extinction coefficient for ice after Grenfell and Maykut (1977)
ρ_i	$900\,kg\,m^{-3}$	Density of ice
L_f	$3.34 \times 10^{5}\,J\,kg^{-1}$	Latent heat of fusion of ice
F_w	$2\,W\,m^{-2}$	Oceanic heat flux to ice (Maykut and Untersteiner, 1971)
q_a		Specific humidity
	1×10^{-3}	Winter
	3×10^{-3}	Summer

2. INTRODUCTION

Statistical analyses of sea-ice prediction (ice-edge location and area concentration) suggest that sea ice is predictable weeks and months in advance, given present anomaly fields (deviations from climatology) for one or more of the atmosphere, cryosphere and hydrosphere (Walsh and Johnson, 1979; Walsh, 1980; Chapman and Walsh, 1991; Marsden and others, 1991). Specific anomaly fields considered have included ice extent, surface salinity,

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50 m temperature, 400–600 m salinity (Marsden and others, 1991), ice area, sea-surface temperature, 700 mbar pressure field and surface-air temperature (Chapman and Walsh, 1991), surface temperature and sea-level pressure (Walsh, 1980), surface temperature, sea-level pressure, 700 mbar heights and temperatures (Walsh and Johnson, 1979). The apparent successes of the statistical analyses suggest that model-based ice forecasting might be successful on similar time-scales. Determining how far into the future such a forecast might be skillful (more accurate than climatology) is one purpose here.

An ice-model experiment (Hibler and Walsh, 1982) finds a significant correlation, 0.48, for a thermodynamics-only prediction of the Arctic ice-edge location. Adding dynamics increases the correlation to 0.58, which suggests that the dynamics are helpful but that much of the predictive skill lies with the thermodynamics.

An ice-thermodynamics model is taken to examine reasons for the predictability of sea ice. Specific features to be understood are: why is the present ice anomaly a better predictor (providing a more accurate forecast than climatology for a longer period, i.e. more skillful) than atmospheric anomalies (Walsh and Johnson, 1979; Walsh, 1980; Johnson and others, 1985); why is the time-scale of prediction weeks rather than days as it is for the atmosphere; and why is the time-scale of predictability longer in the spring and summer melt season than in the fall and winter freezing season. Since an incomplete physical model is taken here, rigorous answers to these questions are not possible. It is suggested, though, that if characteristics are found while examining the thermodynamic processes alone which are similar to the characteristics observed in Nature, then Nature is governed by thermodynamics in those situations.

3. ICE-THICKNESS DISTRIBUTION

An icepack is composed of many thicknesses of ice. We prefer to treat the icepack as a continuum, which means that we view the ice at a scale which is large compared to the size of individual floes. Consequently, each region of the continuum also contains floes of many different thicknesses. Certain thermodynamic processes, such as the conduction of heat through the ice, are sensitive to ice thickness. So, we need to track the fraction of the area of any region which is covered by ice of a given thickness. This gives rise to the notion of an ice-thickness distribution (Thorndike and others, 1975) $g(x, y, t; h)$. The fraction of area centered at location x, y at time t which is covered by ice between thickness h and $h + \mathrm{d}h$ is given by g. The ice-thickness distribution will change due to thermodynamic effects (freezing and melting) and dynamical effects (ridging, rafting and crushing). Only the thermodynamic part of the evolution equation for the ice-thickness distribution will be used as the basis for analysis in this study.

The thermodynamics-only ice-thickness distribution evolution is given by

$$\frac{\partial g}{\partial t} + \frac{\partial fg}{\partial h} = 0 \qquad (1)$$

after Thorndike and others (1975) but neglecting lateral

ice freezing. f is the rate of freeze or melt, in m s^{-1}, of ice with thickness h.

Consider the meaning of climatology in this context. Climate refers to some typical annual cycles in both g and f, which will be denoted by $\bar{g}$ and $\bar{f}$. Also, the definition is required that:

$$\frac{\partial \bar{g}}{\partial t} + \frac{\partial \bar{f}\bar{g}}{\partial h} = 0 \qquad (2)$$

which includes the approximation that the mean of the products is equal to the product of the means.

Anomalies in ice extent or coverage will appear as anomalies in g. Thus, $g = \bar{g} + g'$, where g' are the anomalies. Atmospheric or oceanic anomalies, such as a warm summer or cold winter, will contribute to f'. Note that the anomalies from the atmosphere and ocean are only important to this model in so far as they affect the freezing or melting rate of the ice. The freezing rate and ice-thickness perturbations are not necessarily small. Near the ice edge, they are always large (the climatic term is near-zero). In order to examine the physical processes which are most important, Equation (1) will be linearized.

Here, $\bar{f}$ is considered known and is uncoupled from the ice-thickness distribution g. So we lack non-linear feed-back, the element which usually limits predictability. Consider instead the ice-thickness distribution perturbation, g'. If g' is smaller than our ability to distinguish it from zero, and hence our ability to distinguish g from $\bar{g}$, then predictability is lost. In this case, climatology is equally as good as the model at forecasting the distribution at this future time. Conversely, consider an initial state which contains an unmeasurably small error. If that perturbation grows large enough to be measurable, predictive skill is lost.

Now let us examine the perturbation equation derived by substituting $g = \bar{g} + g'$ and $f = \bar{f} + f'$ into Equation (1), suggestively rewritten, including both processes:

$$\frac{\partial g'}{\partial t} + \left[(\bar{f} + f')\frac{\partial g'}{\partial h} + f'\frac{\partial \bar{g}}{\partial h} \right] \\ + \left[g'\frac{\partial(\bar{f} + f')}{\partial h} + \bar{g}\frac{\partial f'}{\partial h} \right] = 0 \qquad (3)$$

where the identity from Equation (2) has already been applied. The first bracketed term represents a one-dimensional wave equation for the thickness distribution propagating through time and thickness. The first half gives the propagation speed of thickness anomalies, while the second describes the perturbations due to a perturbed propagation rate of the climatological thickness distribution. The wave-like nature of this term was discussed by Coon and others (1974). The second bracketed term describes an anomaly dissipation or growth term. The first part amplifies (since $\partial f/\partial h$ is normally non-positive) the perturbation g'. The second part of the term contributes anomalies due to anomalous dispersion of the climatological thickness distribution.

The wave-like term suggests high predictability. Given f' and $\bar{f}$, g can be computed indefinitely into the future without g' decaying or growing. The purely propagating term has no means of amplifying or

shrinking the perturbations. For example, consider the thickness at which g' is largest. At that thickness $\partial g'/\partial h$ is zero. So the advection is also zero and the wave term cannot change g' at that location.

The second terms provide means for predictive skill to be lost. The second term within brackets provides a mechanism for g' to grow through the production of thickness anomalies due to anomalous dispersion of the climatological thickness distribution. The first term within the second bracket provides a means of error growth through amplification of the perturbation in g'. This perturbation means that there is excess or deficit area being covered by ice between two thicknesses. The thinner ice grows more rapidly than the thicker ice so, after some time, the same area of perturbation is confined into a narrower band of thicknesses. g' must therefore be larger, because its integral over thickness must equal the same area for the perturbation as before the perturbed ice was allowed to grow. The argument applies to melting as well, with the thicker ice melting more rapidly. The e-folding time for perturbation growth by this means is $|(\partial f/\partial h)|^{-1}$, which varies from hours to years depending on the thickness and the season. The concentration of the perturbation into an ever-smaller range of thicknesses can be thought of as a negative dispersion.

4. PREDICTABILITY

Now we can begin to address the question of why the ice-edge location is more accurately forecast or accurately forecast further into the future when using ice-anomaly fields rather than atmospheric anomaly fields. Consider a (finite) perturbation to the ice-thickness distribution in the presence of a climatological atmosphere ($f' \equiv 0$). The evolution of the perturbation will be

$$\frac{\partial g'}{\partial t} + \overline{f}\frac{\partial g'}{\partial h} + g'\frac{\partial \overline{f}}{\partial h} = 0. \tag{4}$$

During the freezing season, $\overline{f}$ is positive and decreases monotonically with h. So $\partial \overline{f}/\partial h$ is strictly negative and will amplify perturbations. For illustrative purposes, the ice-growth/decay model discussed in the next section has been used to derive freezing and melting rates for winter and summer conditions, respectively. The freezing and melting rates so derived are illustrated in Figure 1. The assumed winter and summer conditions have been given above. For $\overline{f}$ proportional to $\alpha h^{-\beta}$, the approximate form of $\overline{f}$ found by curve-fitting the winter freezing rates illustrated in Figure 1, the e-folding period is $h^{1+\beta}/(\alpha\beta)$. Typical values are $\alpha = 1.37$ and $\beta = 0.82$, where time is in days and thickness is in centimeters. Note that the length of predictive skill increases rapidly for increasingly thick ice. Under a climatological atmosphere, the ice-thickness distribution-adjustment time-scale is about 20 h for 10 cm thick ice, 64 h for 20 cm ice, 20 d for 60 cm thickness and 1.3 years for 3 m thick ice. The latter thicknesses correspond to mean thicknesses of the Antarctic (Wadhams and others, 1987) and the Arctic (Bourke and Garrett, 1987), respectively.

Now, consider the early (i.e. linearizeable) growth of perturbations to the sea-ice thickness distribution due to
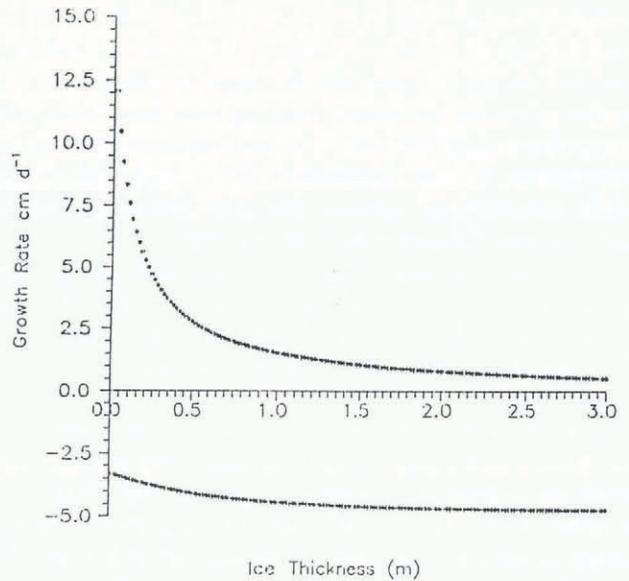

Fig. 1. Freezing rate in cm d⁻¹ as a function of thickness in meters for winter (upper curve) and summer (lower curve).

freezing-rate anomalies

$$\frac{\partial g'}{\partial t} + \frac{\partial g'\overline{f}}{\partial h} = -\frac{\partial f'\overline{g}}{\partial h}. \tag{5}$$

The growth of the ice-thickness anomalies, g', is accomplished through either negative dispersion of the perturbation with respect to thickness (the second term in Equation (5)), or by anomalous propagation and dispersion of the climatological thickness distribution (the third term). The equilibrium response in g' to an anomaly in freezing is $g' = (-f'/\overline{f})\overline{g} + C$ where C is a constant of integration which is taken as zero to satisfy area conservation. For sufficiently small f', g' is never large. For $\overline{g}$ small, g' is also constrained to be small. The only time or place that g' may be large is when f' is large and $\overline{f}$ is small, namely where the deviation from climatological freezing rates is large and the climatological freezing rate itself is small. This places us in the marginal ice zone during a time of anomalously cold weather. In the interior icepack, then freezing-rate anomalies are usually unable to produce large anomalies in ice-thickness distribution (g is large but f' is thickness-dependent, decreasing with thickness and the thickness is large).

Now, consider the relative roles of f' and $\overline{f}$. f' acts to introduce anomalies into the ice-thickness distribution by perturbing the climatological cycle of ice growth and decay. Once an ice-thickness anomaly is produced, the climatological freezing rates propagate the change through thickness at a rate f and concentrate it into an increasingly narrow thickness range at a rate proportional to $|(\partial \overline{f}/\partial h)|^{-1}$. This allows us to answer the question of why a present ice-anomaly field is a more skillful ice predictor than the atmospheric anomaly is. The amplification of an anomaly in the ice distribution occurs on a time-scale of $|(\partial \overline{f}/\partial h)|^{-1}$. The production of an ice-thickness distribution anomaly, on the other hand, occurs on the time-scale of $|(\partial f'/\partial h)|^{-1}$, which will generally exceed the amplification period. If we already know that the thickness distribution is perturbed (again, thick ice

will be most important), this distribution can be predicted well into the future as we now start with g' being zero and can successfully compute the thickness distribution out to a time when the anomalous freezing rates have produced a significant perturbation. The instantaneous state of the atmosphere is only predictable for a couple of weeks, while anomalies in ice-cover concentration ice persist for up to a year (Marsden and others, 1991).

We also see from Figure 1 why there is greater predictability in the melt season than in the freezing season. Figure 1 presents melting and freezing rates as a function of thickness for summer and winter; physical parameters are given in section 1. The melt rate is far less dependent on thickness than the freezing rate. Except for ice thinner than, say, 50 cm, the freezing rate is essentially thickness-independent. Figure 2 presents $|(\partial f/\partial h)|^{-1}$ for summer and winter conditions, showing that it is far larger in summer than winter. For summer melt rates, the predictive scale for 60 cm ice is 2.2 years, and 361 years for 3 m thick ice, as opposed to 20 d and 1.3 years for freezing, respectively. The summer predictive time-scale is far longer than the time required to melt all the ice (or for summer to end). So, the thermodynamics do not limit predictive skill in the summer or for the thickest ice in winter.

Ocean anomalies, such as an anomalously low-salinity or warm upper layer, affect predictability only indirectly. The contribution of the ocean to the ice-heat balance, and hence freezing/melting rates, is thickness-dependent. So, the ocean makes no contribution to the dispersion term. The ocean can affect predictability by acting to produce thicker or thinner ice. As already seen, thinner ice is less predictable. So, if the ocean were warmer, giving rise to a thinner ice cover, the predictability period for the ice would be decreased. The quantity of interest here is the heat flux from the ocean to the ice.

From our analysis of anomaly preservation, a predictive time-scale of several weeks (Walsh and Johnson, 1979; Walsh, 1980; Chapman and Walsh, 1991; Marsden and others, 1991) suggests that the most important ice is thick, over, say, 50 cm (2 week winter
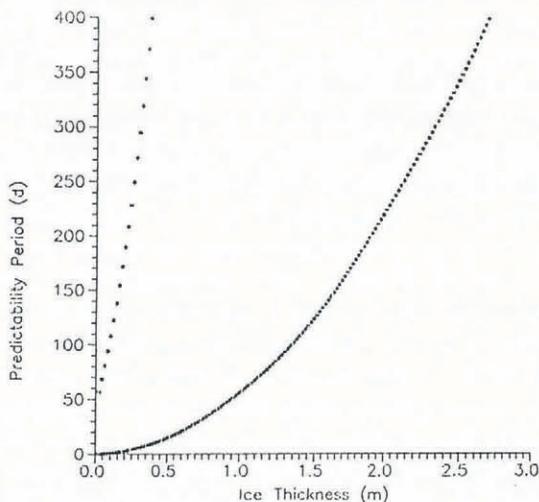
predictability). Both Arctic and Antarctic icepacks have a wintertime mean thickness greater than this, which corroborates our expectation.

5. FREEZING-RATE SENSITIVITY TO THE ATMOSPHERE AND OCEAN

A closer examination of the ice thermodynamics is now in order. Figure 3 illustrates the thermodynamic terms involved in ice-floe freezing and melting. The formulation of the thermodynamics follows the zero-level version of Semtner's (1976) solution, except that penetrating shortwave radiation is used to melt the ice as a whole rather than in forming an internal energy store.

$$H\downarrow \quad LE\downarrow \quad \epsilon_i LW\downarrow \quad \epsilon_i\sigma T_S^4\uparrow \quad (1-\alpha)(1-I_0)SW\downarrow$$

Conduction$\uparrow$ $\quad \beta_s I_0(1-\alpha)SW\downarrow$

SNOW

Conduction$\uparrow$ $\quad (1-\beta_s)\beta_i I_0(1-\alpha)SW\downarrow$

ICE

$$FW\uparrow \quad (1-((1-\beta_s)\beta_i))I_0(1-\alpha)SW\downarrow$$
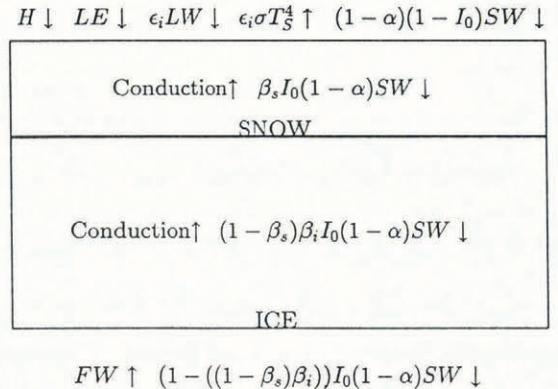
Fig. 3. Diagram of ice-thermodynamic variables. H is the sensible-heat flux, LE is the latent-heat flux, LW is the longwave-energy flux away from the ice, $\epsilon_i\sigma T_s^4$ is the longwave-energy flux away from the ice, SW is the down-welling shortwave energy, α is the albedo, I_0 is the fraction of the shortwave energy which penetrates the surface, β_s is the fraction of down-welling shortwave energy which is absorbed in the snow layer (if any), β_i is the fraction of down-welling shortwave energy which is absorbed in the ice and FW is the heat flux from the ocean to the ice. Energy fluxes are measured negative towards the ice.

In the winter (freezing conditions), the ice-surface fluxes are forced to sum to zero by adjusting the surface temperature to provide flux balance. The contributing fluxes are: sensible-heat flux (H), latent-heat flux (LE), conductive-heat flux (K), down-welling longwave-radiation flux ($LW\downarrow$), up-welling longwave-radiation flux ($LW\uparrow$) and absorbed shortwave-radiation flux (SW_{net}). We formulate the fluxes as:

$$H = \rho_a U_a C_h C_p (T_s - T_a) \tag{6}$$

$$LE = \rho_a U_a C_q L_v (q_s(T_s) - q_{10}(T_a)) \tag{7}$$

$$K = -k_s k_i (T_f - T_s)/(k_s H_i + k_i H_s) \tag{8}$$

$$LW\downarrow = -(0.7855 + 0.2232C^{2.75})\epsilon_i\sigma T_a^4 \tag{9}$$

$$LW\uparrow = \epsilon_i\sigma T_s^4 \tag{10}$$

$$SW_{net} = -(1-\alpha)SW\downarrow$$
$$\cdot (1 - I_0\exp(-(H_s\tau_s + H_i\tau_i))) \tag{11}$$

Fig. 2. e-folding period in days of errors in the ice-thickness distribution as a function of ice thickness in meters. Upper curve is for summer conditions, lower curve is for winter conditions.

where k_s and k_i are the thermal conductivities of snow and ice, respectively, H_s and H_i are the thicknesses of snow and ice, respectively, T_f is the freezing temperature of sea water, T_s is the surface temperature of the floe, C_h is the bulk-transfer coefficient for sensible heat, C_q is the bulk-transfer coefficient for latent heat, U_a is the atmospheric wind speed at 10 m, C_p is the specific heat of air, L_v is the latent heat of vaporization of ice, q_s is the saturation water-vapor content at temperature T_s, q_{10} is the actual water-vapor content at 10 m, ϵ is the longwave emissivity of the surface (snow or ice), C is the cloud-cover fraction, α is the surface albedo, $SW\downarrow$ is the down-welling shortwave-radiation flux, I_0 is the fraction of incident solar radiation which penetrates the surface and τ_s and τ_i are the shortwave-extinction coefficients for snow and ice, respectively. The longwave down-welling flux relation is the empirical relation due to Maykut and Church (1973). The convention that fluxes are positive away from the ice is assumed.

The freezing rate (m s^{-1} of ice thickening) has been given by Semtner (1976):

$$f = \frac{\partial H_i}{\partial t} = (-F_w + k_s k_i (T_f - T_s)/(k_s H_i + k_i H_s))$$
$$/(\rho_i L_f) \qquad (12)$$

where F_w is the oceanic heat flux into the ice. Note that this may produce basal melting when the conduction is slow, either because of thick snow and ice or because of warm surfaces. In summer, T_s is limited to the freezing point of the ice and excess flux into the ice results. This flux is balanced by increased melting:

$$f = \frac{\partial H_i}{\partial t} = (-F_w + Q_{extra})/(\rho_i L_f) \qquad (13)$$

where Q_{extra} is the sum of the surface-flux terms at $T_s = T_f$. The thermodynamic picture used here is not strictly accurate in the freezing season for ice thinner than about 50 cm or in the summer-melt season. Under these conditions, certain mechanical processes (rafting of small floes and formation of brine channels and subsequent mechanical break-up) have potentially significant effects on the ice physics (Maykut, 1986). Nonetheless, the larger-scale considerations of thermodynamics do apply, in that even though brine channeling may permit melt without changing the thickness of the ice, the volume of ice melted still corresponds to that which would be expected thermodynamically. Values of the constants have already been given.

Equations (12) and (13) give the freezing or melting rate (f) after T_s has been determined from Equations (6)–(11). Our main interest in terms of sea-ice predictability is $|(\partial f/\partial h)|^{-1}$. For winter, after differentiating Equation (12) with respect to H_i, and recalling that the surface temperature can depend on ice thickness, we find

$$\left(\frac{\partial f}{\partial h}\right)^{-1} = -\frac{\rho_i L_f (k_s H_i + k_i H_s)}{k_s k_i}$$
$$\cdot \left[\frac{(T_f - T_s)k_s}{k_s H_i + k_i H_s} + \frac{\partial T_s}{\partial H_i}\right]^{-1} \qquad (14)$$

where

$$\frac{\partial T_s}{\partial H_i} =$$
$$\frac{\left[\frac{(T_f - T_s)k_s^2 k_i}{(k_s H_i + k_i H_s)^2} - (1 - \alpha)SW\downarrow I_0 \tau_i \exp(-H_s \tau_s + H_i \tau_i))\right]}{\frac{-k_s k_i}{(k_s H_i + k_i H_s)} + \rho_a C_q L_v U_a \frac{\partial q_s}{\partial T_s} \rho_a C_D C_p U_a + 4\epsilon o T_s^3}.$$
$$(15)$$

The salient feature of Equation (15) is that the ice surface cools for thicker ice. Therefore, the ice-freezing rate is less dependent on thickness than if T_s were thickness-independent. This gives a longer period of predictability. In the summer, T_s is fixed by the freezing point, so the $\partial f/\partial h$ is given by

$$\left(\frac{\partial f}{\partial h}\right)^{-1} = \rho_i L_f \left(\frac{\partial Q_{extra}}{\partial h}\right)^{-1} \qquad (16)$$

where

$$\frac{\partial Q_{extra}}{\partial h} = -(1 - \alpha)SW\downarrow I_0 \tau_i \exp(-(h_s \tau_s + h_i \tau_i)), \quad (17)$$

so we see that in summer the only dependence of melt rate on ice/snow thickness comes about from the additional shortwave radiation absorbed by thicker ice. Since $\partial Q/\partial h$ is an exponential function of thickness, it is only for thin ice that the melt rate becomes sensitive to thickness. Hence, the summer ice has an extremely long predictability period. Returning to Figure 2 shows that the period estimated for predictability is longer than the period required to melt the entire floe under the presumed conditions.

6. DISCUSSION

This analysis suggests answers to some questions which are important to understanding and forecasting sea-ice conditions. First, it is apparent from earlier work that the time-scale of sea-ice anomaly persistence is weeks to months (Walsh and Johnson, 1979; Walsh 1980; Chapman and Walsh, 1991; Marsden and others, 1991). We see here that this is expected for regions of thick ice, as this ice can respond only slowly to atmospheric anomalies. The length of ice-anomaly persistence is longer in the melt season than in the freezing season because the freezing process is more thickness-dependent than melting (larger df/dh). The relative ease with which ice anomalies (once formed) are predicted suggests that statistical forecasting models such as autoregressive models of ice anomalies are liable to be more accurate than climatology for longer lead times than a regression of the ice anomaly based on past atmospheric anomalies, in accord with experience (Walsh and Johnson, 1979; Walsh, 1980; Johnson and others, 1985).

Another feature of operational interest is that, given knowledge of the atmosphere, we can also estimate the period for which an ice-thickness forecast may be expected to be better than climatology due to thermodynamics. The estimates are high, years in the summer versus weeks inferred by studies (cf. Walsh and Johnson, 1979; Walsh, 1980; Chapman and Walsh, 1991; Marsden and others, 1991). The likely candidate for the discrep-

ancy is the absence of dynamics in this analysis. For a large-scale icepack, convergence is of the order of $10^{-2}\,\mathrm{d}^{-1}$ (Coon and others, 1974), which corresponds to a 100 d predictability limit. This limit is reached by ice thicknesses of 10 cm in the summer and 1.36 m in the winter. So, it is suggested that these are the conditions which contribute to the observed characteristics of sea-ice predictability.

Ice dynamics are definitely an important element in ice prediction. In the long term and large scale, dynamics limit the prediction range. At small scales and short range, when divergence can be much larger, dynamics again limit the prediction range. Further, via ridging, dynamics will affect the ice-thickness distribution — removing ice from thin classes and pushing it into thick classes.

The thermodynamic limit on predictability will be an important consideration for predicting thin ice in the melt season, or with new, young or first-year ice in the winter. For operational ice prediction, this suggests that forecast range in the winter is limited by the ability to predict the freezing of thinner ice. The next step in this work will be to examine the combined effects of dynamics and thermodynamics on ice predictability.

ACKNOWLEDGEMENTS

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