Banner appropriate to article type will appear here in typeset article

Guidelines for authors

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- 3 ¹STM Journals, Cambridge University Press, The Printing House, Shaftesbury Road, Cambridge CB2
- 4 8BS, UK
- 5 ²DAMTP, Centre for Mathematical Sciences, Wilberforce Road, Cambridge CB3 0WA, UK
- 6 (Received xx; revised xx; accepted xx)
- 7 This file contains instructions for authors planning to submit a paper to the *Journal of Fluid*
- 8 Mechanics. These instructions were generated in LATEX using the JFM class file, and the source
- 9 files for these instructions can be used as a template for submissions. The present paragraph
- appears in the abstract environment. All papers should feature a single-paragraph abstract
- of no more than 250 words, which provides a summary of the main aims and results. In
- 12 addition to the figures in the main article a graphical abstract is now required. It will be
- 13 used as a small thumbnail in the table of contents and on the abstract page, so multiple
- panels are not suitable and will be rejected. Please confirm that you have included an image
- 15 to accompany your abstract, which will be used as the graphical abstract for manuscripts
- published in 2020. The image must be of aspect ratio 1.2:1 (e.g. 6cm x 5cm) and should
- be submitted in GIF or high resolution JPEG format (300 dpi). Unless very large, vector
- graphics are preferred to ensure image sharpness regardless of sizing. If you do not have
- 19 the copyright to the image, please ensure you have permission to reuse the figure. Captions
- 20 are not required. Text is actively discouraged, but if it must be used, it should be legible
- 21 in a small thumbnail (2.4cmx2cm) presented in the table of contents. All graphical abstract
- 22 images will be considered for a JFM cover selection by the JFM Panel. Please note that we
- 23 publish 24 covers in a year.
- 24 **Key words:** Authors should not enter keywords on the manuscript, as these must be chosen by
- 25 the author during the online submission process and will then be added during the typesetting
- 26 process (see Keyword PDF for the full list). Other classifications will be added at the same
- 27 time.

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MSC Codes (Optional) Please enter your MSC Codes here

29 1. How to submit to the Journal of Fluid Mechanics

- 30 Authors must submit using the online submission and peer review system Scholar One
- 31 (formerly Manuscript Central). If visiting the site for the first time, users must create a
- 32 new account by clicking on 'register here'. Once logged in, authors should click on the
 - † Email address for correspondence: JFMEditorial@cambridge.org

'Corresponding Author Centre', from which point a new manuscript can be submitted, with 33 step-by-step instructions provided. Authors must at this stage specify whether the submission 34 is a JFM Paper, or a JFM Rapids paper (see §4 for more details). In addition, authors must 35 specify an editor to whom the paper will be submitted from the drop-down list provided. 36 Note that all editors exclusively deal with either JFM Paper or JFM Rapids (clearly indicated 37 on the list), so please ensure that you choose an editor accordingly. Corresponding authors 38 39 must provide a valid ORCID ID in order to submit a manuscript, either by linking an existing ORCID profile to your ScholarOne account or by creating a new ORCID profile. Once your 40 submission is completed you will receive an email confirmation. Book reviews should not 41 be submitted via the online submission site, but should instead be submitted by email to 42 anne.juel@manchester.ac.uk. 43

4 2. Rules of submission

Submission of a paper implies a declaration by the author that the work has not previously been published, that it is not being considered for publication elsewhere and that it has not already been considered by a different editor of the Journal. If you have uploaded your manuscript via the arXiv function, then please include your E-print Number during the submission process.

3. Authors responsibilites

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Authors need to declare in their covering letter to the Editor and during the online submission 51 process whether their manuscript had previously been considered for publication in the 52 Journal of Fluid Mechanics. Questions and declarations to that effect must be answered 53 truthfully. Editors, referees, readers and publishers have the right to assume that submitted 54 (and published) manuscripts do not contain scientific dishonesty or fraud comprising, for 55 example, fictitious or manipulated data, plagiarised material (either from previous work of 56 the authors or that of other persons), reference omissions, false priority statements, 'hidden' 57 multiple publication of the same data or incorrect authorship. Authors must not breach any 58 copyright. The Journal of Fluid Mechanics uses the iThenticate software to detect instances 59 of plagiarism in manuscripts submitted to it. 60

3.1. Transparency and Openness Promotion (TOP)

The overarching policy of the *Journal of Fluid Mechanics* is that research articles should contain sufficient information to allow others to understand, replicate and verify findings, and compare them with alternative studies. We therefore require that whenever possible:

Understanding - Articles should be written and will be assessed for clarity, both of the execution of the research and for its outcomes and conclusions.

Replication - All information required to replicate the study must be provided, within the body of the paper and/or publicly accessible repositories. Examples of what is required include but are not limited by:

- for analytical studies, the mathematically complete set of equations and boundary conditions, any theorems relied upon, appropriately referenced;
- for numerical studies, the mathematically complete set of equations and boundary conditions, sufficient descriptions of the algorithms or packages used to solve them, appropriately referenced, and the resolution used with respect to the independent variables;
- for laboratory experiments, the dimensions and construction of any apparatus, the materials used including their relevant physical properties, the protocol adopted for the

running of the experiments, the measurement tools used including their resolution and accuracy, including appropriate calibration standards;

• for field studies, the raw data collected or used, any protocols or tools used to access the data (e.g. data-mining tools) or to process it.

Verification - Most studies can be verified or falsified provided that sufficient detail is given for them to be replicated (see above). Where data is manipulated (for example, bringing together multiple data sets by scaling) the raw (dimensional) data relating to the primary measurements (laboratory) or outputs (numerical) should be provided together with the protocols or tools used to process them.

Comparison - All graphical information should be supplemented with numerical data or precise algorithms to reproduce it. For example, data points should be provided in a spreadsheet and curves should be defined either explicitly with an equation or as resulting from a precisely defined algorithm.

4. Types of paper

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4.1. Standard papers

Regular submissions to JFM are termed 'standard papers'. Note that such papers must contain 92 original research. Papers should be written in a concise manner; though JFM has no page 93 limit, each paper will be judged on its own merits, and those deemed excessive in length will 94

be rejected or will require significant revision. 95

4.2. JFM Rapids

JFM Rapids is devoted to the rapid publication of short, high-impact papers across the full range of fluid mechanics. Manuscripts submitted as JFM Rapids must be strictly 10 or fewer printed pages, and must be submitted in LATEX using the jfm.cls class file, so as to ensure that they meet the page limit and to expedite their production. As with standard papers, the principal and over-riding objective is to publish papers of the highest scientific quality.

Once a paper is submitted, reviewers are asked to provide reports with a short turnaround. In order to be accepted for publication in JFM Rapids, such papers must be strongly endorsed by the referees and should require only minor revisions to improve clarity, usually without recourse to a second round of reviewing. In this case, and at the discretion of the editor, some additional pages may be allowed to address specific points raised by the reviewers, such as the addition of an extra figure or some explanatory text.

Papers that are rejected having been submitted to Rapids are rejected on behalf of the whole Journal and may not be submitted for consideration by another associate editor of JFM, whether for Rapids or as a Standard paper.

In cases where the editor, guided by the reviewers, judges that a paper has merit but requires substantial revision that will require significant reviewing, a decision of 'revise and resubmit' will be given. On re-submission, such papers will be handled as standard JFM papers and if accepted will not subsequently appear as JFM Rapids.

JFM Rapids will be published online within one month of final acceptance. They will appear within a designated section on the Journal of Fluid Mechanics website. Each Rapid will be cited and indexed as a JFM article but with a distinctive Rapids identifier, and will be assigned to a JFM volume.

4.3. JFM Perspectives

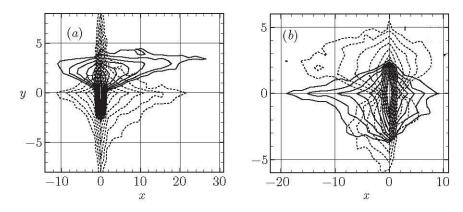


Figure 1: Trapped-mode wavenumbers, kd, plotted against a/d for three ellipses: ---, $b/a = 1; \cdots, b/a = 1.5.$

5. File types

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Authors are strongly encouraged to compose their papers in LATEX, using the jfm.cls style 122 file and supporting files provided, with the ifm-instructions.tex file serving as a template 123 (please note that this is mandatory for JFM Rapids). A PDF of the LATEX file should then be 124 generated and submitted via the submission site. For the review process the pdf file should 125 be no more than 10MB. There is no need to submit the LATEX source files alongside the PDF, 126 but upon provisional acceptance of the paper, the LATEX source files, along with individual 127 figure files and a PDF of the final version, will need to be submitted for typesetting purposes. 128 Authors may also compose standard papers in Word, though this will lead to the paper 129 130 spending a longer period in production. If using Word, please note that equations must NOT be converted to picture format and the file must be saved with the option 'make equation 131 132 editable'. All submitted video abstract files should be formatted as MP4 (H.264). MP4 has full compatibility across commonly used browsers, whereas other video formats will only 133 134 work on selected browsers. This will ensure the greatest possible dissemination of this work.

6. Preparing your manuscript

Authors should write their papers clearly and concisely in English, adhering to JFM's 136 137 established style for mathematical notation, as provided in Section 12. We encourage the submission of online supplementary material alongside the manuscript where appropriate 138 139 (see Section 6.3). Metric units should be used throughout and all abbreviations must be defined at first use, even those deemed to be well known to the readership. British spelling 140 must be used, and should follow the Shorter Oxford English Dictionary.

6.1. Figures

All authors need to acquire the correct permissions and licences to reproduce figures, which 143 should be submitted with the production files. Further information on applying for permission 144 to reuse figures can be found here. Images should be submitted in EPS or high-resolution 145 TIFF format (1200 dpi for lines, 300 dpi for halftone and colour in RGB format, and 600 146 dpi for a mixture of lines and halftone) and all labels should be editable. Unless very large, 147 vector graphics are preferred to ensure image sharpness regardless of sizing. The minimum 148 acceptable width of any line is 0.5pt. Each figure should be accompanied by a single caption, 149 to appear beneath, and must be cited in the text. Figures should appear in the order in which 150 they are first mentioned in the text and figure files must be named accordingly ('Abstract.eps, 151

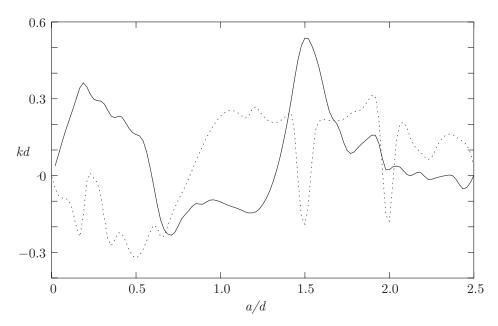


Figure 2: The features of the four possible modes corresponding to (a) periodic and (b) half-periodic solutions.

a/d	M = 4	M = 8	Callan et al.
0.1	1.56905	1.56	1.56904
0.3	1.50484	1.504	1.50484
0.55	1.39128	1.391	1.39131
0.7	1.32281	10.322	1.32288
0.913	1.34479	100.351	1.35185

Table 1: Values of kd at which trapped modes occur when $\rho(\theta) = a$.

Fig1.eps', 'Fig2a.tiff', etc) to assist the production process (and numbering of figures should continue through any appendices). Words *figure 1, table 1 and movie 1* should be lower case. For example see figures 1 and 2. Failure to follow figure guidelines may result in a request for resupply and a subsequent delay in the production process. Note that *all* figures will be relabelled by the typesetter, so please ensure all figure labels are carefully checked against your originals when you receive your proofs.

158 6.2. *Tables*

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Tables, however small, must be numbered sequentially in the order in which they are mentioned in the text. Words *table 1*, *table 2* should be lower case throughout. See table 1 for an example.

6.3. Online supplementary material

Relevant material which is not suitable for inclusion in the main article, such as movies or numerical simulations/animations, can be uploaded as part of the initial submission. Movies must be submitted in .mp4 format and have the file designation of 'Movie'. Each movie must be numbered in the order they are mentioned and titled movie 1, movie 2 etc and accompanied

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by a separate caption. To ensure maths terms display correctly they should be bounded by 167 \$\$ and written in TeX, e.g. movie 1. Side view of numerical Schlieren contours from case 168 E1N at z = Lz/2. Each movie should be no more than 50MB. Upon publication these 169 materials will then be hosted online alongside the final published article. Likewise, should 170 there be detailed mathematical relations, tables or figures which are likely to be useful only 171 to a few specialists or take up excessive space in the article, these should also be published 172 173 online as supplementary material [designated as 'Other supplementary material']. Note that supplementary material is published 'as is', with no further intervention made during the 174 175 Production process, all 'draft' information should be removed.

7. Editorial decisions

7.1. *Revision*

If a revision is requested, you should upload revised files following the same procedure as 178 for submitting a new paper. You begin by clicking on 'Manuscripts with decision' in your 179 Corresponding Author Centre, and then on 'Create a revision'. (Note that if you abandon the 180 process before completing the submission, to continue the submission, you must click on 181 'Revised manuscripts in draft'.) There is a new first page showing the decision letter and a 182 space for your reply to the reviewer's/editor's comments. You also have the opportunity at 183 this stage to upload your reply to the comments as separate files. All the values filled in on 184 original submission are displayed again. The ID number of the paper will be appended '.R1'. 185 Also note that if a manuscript is submitted as a *JFM Rapid*, but requires substantial revision, 186 it will be re-designated as a standard paper, and the ID and paper type will be amended to 187 reflect this. 188

7.2. Provisional acceptance

If the paper is accepted as suitable for publication you will be sent a provisional acceptance 190 191 decision. This enables you to upload the final files required for production: (1) the final PDF 192 or word version of the paper, designated as a 'Main Document'; (2) any source files (see section 5) which must be designated as 'Production Files' and uploaded as a single .zip or 193 .tar file; (3) a completed author publishing agreement form which is available to download 194 at Cambridge Core. For Open Access there is a one-off fee, further information can be found 195 at JFM open access - FAQs. If your research is publicly funded and your organisation comes 196 under one of Cambridge University Press's Read and Publish agreements you may be entitled 197 to free Open Access. Please check your eligibility here. 198

7.3. Acceptance

On receipt of the production files you will be sent an email indicating completion of the acceptance process.

8. Publication process

Once a paper has been accepted for publication and the source files have been uploaded, the manuscript will be sent to Cambridge University Press for copyediting and typesetting, and will be assigned a digital object identifier (doi). When the proof is ready, authors will receive an email alert containing a link to the PDF of the proof, and instructions for its correction and return. It is imperative that authors check their proofs closely, particularly the equations and figures, which should be checked against the accepted file, as the production schedule does not allow for corrections at a later stage. Once ready, papers will be published

- online on Cambridge Core in the current 'open' volume. Each volume will be kept open
- 211 for approximately two weeks. Note that the PDF published online is the Version of Record
- and no further alterations/corrections to this document will be allowed. The corresponding
- 213 author is emailed a link to the published article when it is published online.

9. Corrigenda

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- 215 The Journal will publish corrigenda that alter significant conclusions made in a paper. Such
- 216 corrigenda should be submitted to an associate editor, who will consider the submission
- similarly to a new paper and may consult referees if appropriate. When published, corrigenda
- are clearly linked with the original articles to which they refer, and the articles to them.
- The Journal does not normally publish corrigenda to amend typographical errors, so it is
- extremely important that authors make very careful checks of their manuscript at every stage,
- including the reading of proofs, prior to publication.

222 10. Obtaining help

- 223 Technical support for the online submission system is available by clicking on the 'Get Help
- Now' link at the top-right corner of each page of the submission site. Any other questions
- 225 relating to the submission or publication process should be directed to the JFM Editorial
- 226 Assistant, Mrs Amanda Johns, at JFMEditorial@cambridge.org.

227 11. Cambridge Author Services - in partnership with American Journal Experts

- We suggest that authors whose first language is not English have their manuscripts checked
- by a native English speaker before submission. This is optional but will help to ensure that
- any submissions that reach peer review can be judged exclusively on academic merit. Further
- 231 information can be found at Language services, and we suggest that authors make contact as
- appropriate. Please note that use of language editing services is voluntary and at the author's
- 233 own expense. Use of these services does not guarantee that the manuscript will be accepted
- 234 for publication nor does it restrict the author to submitting to a Cambridge-published journal.

12. Notation and style

- 236 Generally any queries concerning notation and journal style can be answered by viewing
- 237 recent pages in the Journal. However, the following guide provides the key points to note. It
- is expected that Journal style and mathematical notation will be followed, and authors should
- 239 take care to define all variables or entities upon first use. Also note that footnotes are not
- 240 normally accepted. Abbreviations must be defined at first use, glossaries or lists/tables of
- abbreviations are not permitted.

12.1. Mathematical notation

- 12.1.1. Setting variables, functions, vectors, matrices etc
 - ullet Italic font should be used for denoting variables, with multiple-letter symbols avoided except in the case of dimensionless numbers such as Re, Pr and Pe (Reynolds, Prandtl,
- and Péclet numbers respectively, which are defined as \Rey, \Pran and \Pen in the template).
 - **Upright Roman font** (or upright Greek where appropriate) should be used for:

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250 (i) (vI) label, e.g. T. t (transpose)
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252 (ii) Fixed operators: \sin , \log , d, Δ , \exp etc.

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(iii) Constants: i $(\sqrt{-1})$, π (defined as \upi),e etc.

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- (iv) Special Functions: Ai, Bi (Airy functions, defined as \Ai and \Bi), Re (real part, defined as \Real), Im (imaginary part, defined as \Imag), etc.
- defined as \Real), Im (imaginates)
 (v) Physical units: cm, s, etc.
 - (vi) Abbreviations: c.c. (complex conjugate), h.o.t. (higher-order terms), DNS, etc.
 - **Bold italic font** (or bold sloping Greek) should be used for vectors (with the centred dot for a scalar product also in bold): $i \cdot j$

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- **Bold sloping sans serif font**, defined by the \mathsfbi macro, should be used for tensors and matrices: **D**
- Calligraphic font (for example \mathcal{G}, \mathcal{R}) can be used as an alternative to italic when the same letter denotes a different quantity use \mathcal in LATEX)
- 271 12.1.2. *Other symbols*
- Large numbers that are not scientific powers should not include commas, but should use a
- 273 non-breaking space, and use the form 1600 or 16 000 or 160 000. Use O to denote 'of the
- order of', not the LATEX O.
- The product symbol (x) should only be used to denote multiplication where an equation
- is broken over more than one line, to denote a cross product, or between numbers . The •
- 277 symbol should not be used, except to denote a scalar product of vectors specifically.

278 13. Citations and references

- All papers included in the References section must be cited in the article, and vice versa.
- 280 Citations should be included as, for example "It has been shown (Rogallo 1981) that..." (using
- 281 the \citep command, part of the natbib package) "recent work by Dennis (1985)..." (using
- 282 \citet). The natbib package can be used to generate citation variations, as shown below.
- 283 \citet[pp. 2-4]{Hwang70}:
- 284 Hwang et al (1970, pp. 2-4)
- 285 \citep[p. 6]{Worster92}:
- 286 (Worster 1992, p. 6)
- 287 \citep[see][]{Koch83, Lee71, Linton92}:
- 288 (see Koch 1983; Lee 1971; Linton and Evans 1992)
- 289 \citep[see][p. 18]{Martin80}:
- 290 (see Martin 1980(@, p. 18)
- 291 \citep{Brownell04,Brownell07,Ursell50,Wijngaarden68,Miller91}:
- 292 (Brownell 2004; Brownell and Su 2007; Ursell 1950; Wijngaarden 1968; Miller 1991)
- 293 (Briukhanovetal et al 1967)
- 294 Bouguet (2008)
- 295 (Josep and Saut 1990)
- The References section can either be built from individual \bibitem commands, or can be
- built using BibTex. The BibTex files used to generate the references in this document can be

- 298 found in the zip file ifm-ifcs.
- Where there are up to ten authors, all authors' names should be given in the reference list.
- Where there are more than ten authors, only the first name should appear, followed by et al.
- JFM discourages citations of manuscript posted on social media sites (such as Research-
- Gate) or on pre-print servers (e.g. ArXiv), that have not been peer-reviewed or published in journals.
- 304 **Supplementary data.** Supplementary material and movies are available at
- 305 https://doi.org/10.1017/jfm.2019...
- 306 Acknowledgements. Acknowledgements may be included at the end of the paper, before the References
- 307 section or any appendices. Several anonymous individuals are thanked for contributions to these instructions.
- 308 **Funding.** Please give details of any financial support.
- 309 **Declaration of interests.** A **Declaration of interests** statement is now mandatory in the manuscript PDF.
- 310 Please included a statement in your manuscript at the end of the main text with regards to any known
- 311 competing financial interests or personal relationships that could appear to have influenced the work reported
- in this paper. These must also be declared in your covering letter to the Editor. Please note that if there are
- 313 no conflicts of interest, the declaration in your PDF should read as follows: Declaration of Interests. The
- 314 authors report no conflict of interest.
- 315 Data availability statement. The data that support the findings of this study are openly available in
- 316 [repository name] at http://doi.org/[doi], reference number [reference number].
- 317 Author ORCID. Authors may include the ORCID identifiers as follows. F. Smith, https://orcid.org/0000-
- 318 0001-2345-6789; B. Jones, https://orcid.org/0000-0009-8765-4321
- 319 Author contributions. Authors may include details of the contributions made by each author to the
- 320 manuscript, for example, "A.G. and T.F. derived the theory and T.F. and T.D. performed the simulations. All
- 321 authors contributed equally to analysing data and reaching conclusions, and in writing the paper."

322 14. Appeals process

- 323 The Journal of Fluid Mechanics has an appeal procedure which provides authors with the
- 324 opportunity to respond to the editorial decision on their manuscript, should they think that
- 325 their manuscript was treated in an unfair manner during the peer-review process. Authors
- 326 have the right to appeal to the Editor or Editor-in-Chief against any decision taken on their
- manuscript at any stage. An appeal will be considered at the direction of the Editorial Board
- 328 of the Journal.

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14.1. How do I appeal?

- Step 1. Requests to have the decision on a submission re-considered should be made in the first instance to the Associate Editor who handled the submission and made the decision. Send a rebuttal letter to the Associate Editor, explaining clearly why you disagree with the decision on your manuscript and including a detailed response to any points of contention in the referees' reports. The Associate Editor will consider your appeal and either invite you to
- the referees' reports. The Associate Editor will consider your appeal and either invite you to submit a revised paper or confirm the original decision.
 - **Step 2.** In case you remain unsatisfied with the Associate Editor's response after Step 1 or at any stage should you consider that your submission was treated unfairly, you should send a letter of appeal to the Editor-in-Chief via the Journal email (JFMEditorial@cambridge.org). Your letter should explain clearly the grounds for your appeal.
- Step 3. The Editor-in-Chief will consider the grounds of your appeal and if he considers there to be a *prima facie* case to consider may assign one of the Deputy Editors to consider the appeal in detail. All appeal requests are handled on a case by case basis and the Deputy Editor's or Editor-in-Chief's decision is final. Appeals are normally considered on the basis

of whether or not the process of review was conducted appropriately. Papers will not routinely be sent for further review.

346 Appendix A.

This appendix contains sample equations in the JFM style. Please refer to the LATEX source file for examples of how to display such equations in your manuscript.

$$(\nabla^2 + k^2)G_s = (\nabla^2 + k^2)G_a = 0 \tag{A1}$$

$$\nabla \cdot \mathbf{v} = 0, \quad \nabla^2 P = \nabla \cdot (\mathbf{v} \times \mathbf{w}). \tag{A 2}$$

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$$G_s, G_a \sim 1/(2\pi) \ln r \quad \text{as} \quad r \equiv |P - Q| \to 0, \tag{A3}$$

$$\frac{\partial G_s}{\partial y} = 0 \quad \text{on} \quad y = 0,
G_a = 0 \quad \text{on} \quad y = 0,$$
(A 4)

$$-\frac{1}{2\pi} \int_{0}^{\infty} \gamma^{-1} [\exp(-k\gamma|y-\eta|) + \exp(-k\gamma(2d-y-\eta))] \cos k(x-\xi) t dt, \qquad 0 < y, \quad \eta < d,$$
353 (A 5)

$$\gamma(t) = \begin{cases} -i(1-t^2)^{1/2}, & t \le 1\\ (t^2-1)^{1/2}, & t > 1. \end{cases}$$
 (A 6)

$$-\frac{1}{2\pi} \int_0^\infty B(t) \frac{\cosh k\gamma (d-y)}{\gamma \sinh k\gamma d} \cos k(x-\xi) t \, dt$$

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$$G = -\frac{1}{4}i(H_0(kr) + H_0(kr_1)) - \frac{1}{\pi} \int_0^\infty \frac{e^{-k\gamma d}}{\gamma \sinh k\gamma d} \cosh k\gamma (d-y) \cosh k\gamma (d-\eta) \quad (A7)$$

Note that when equations are included in definitions, it may be suitable to render them in line, rather than in the equation environment: $\mathbf{n}_q = (-y'(\theta), x'(\theta))/w(\theta)$. Now $G_a = \frac{1}{4}Y_0(kr) + \widetilde{G}_a$ where $r = \{[x(\theta) - x(\psi)]^2 + [y(\theta) - y(\psi)]^2\}^{1/2}$ and \widetilde{G}_a is regular as $kr \to 0$. However, any fractions displayed like this, other than $\frac{1}{2}$ or $\frac{1}{4}$, must be written on the line, and not stacked (ie 1/3).

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$$\frac{\partial}{\partial n_q} \left(\frac{1}{4} Y_0(kr) \right) \sim \frac{1}{4\pi w^3(\theta)} \left[x''(\theta) y'(\theta) - y''(\theta) x'(\theta) \right]$$

$$= \frac{1}{4\pi w^3(\theta)} \left[\rho'(\theta) \rho''(\theta) - \rho^2(\theta) - 2\rho'^2(\theta) \right] \quad \text{as} \quad kr \to 0. \quad (A 8)$$

$$\frac{1}{2}\phi_i = \frac{\pi}{M} \sum_{i=1}^{M} \phi_j K_{ij}^a w_j, \qquad i = 1, \dots, M,$$
 (A 9)

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$$K_{ij}^{a} = \begin{cases} \frac{\partial G_{a}(\theta_{i}, \theta_{j})}{\partial G_{a}(\theta_{i}, \theta_{i})} / \partial n_{q}, & i \neq j \\ \frac{\partial G_{a}(\theta_{i}, \theta_{i})}{\partial G_{a}(\theta_{i}, \theta_{i})} / \partial n_{q} + \left[\rho_{i}' \rho_{i}'' - \rho_{i}^{2} - 2\rho_{i}'^{2}\right] / 4\pi w_{i}^{3}, & i = j. \end{cases}$$
(A 10)

$$\rho_l = \lim_{\zeta \to Z_l^-(x)} \rho(x, \zeta), \quad \rho_u = \lim_{\zeta \to Z_u^+(x)} \rho(x, \zeta) \tag{A 11a,b}$$

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$$(\rho(x,\zeta), \phi_{\zeta\zeta}(x,\zeta)) = (\rho_0, N_0)$$
 for $Z_l(x) < \zeta < Z_u(x)$. (A 12)

$$\tau_{ij} = (\overline{\overline{u}_i \overline{u}_j} - \overline{u}_i \overline{u}_j) + (\overline{\overline{u}_i u_j^{SGS} + u_i^{SGS} \overline{u}_j}) + \overline{u_i^{SGS} u_j^{SGS}}, \tag{A 13a}$$

$$\tau_{j}^{\theta} = (\overline{u_{j}}\overline{\theta} - \overline{u_{j}}\overline{\theta}) + (\overline{u_{j}}\theta^{SGS} + u_{j}^{SGS}\overline{\theta}) + \overline{u_{j}^{SGS}}\theta^{SGS}. \tag{A 13b}$$

$$\mathbf{Q}_{C} = \begin{bmatrix} -\omega^{-2}V'_{w} & -(\alpha^{t}\omega)^{-1} & 0 & 0 & 0\\ \frac{\beta}{\alpha\omega^{2}}V'_{w} & 0 & 0 & 0 & i\omega^{-1}\\ i\omega^{-1} & 0 & 0 & 0 & 0\\ iR_{\delta}^{-1}(\alpha^{t} + \omega^{-1}V''_{w}) & 0 & -(i\alpha^{t}R_{\delta})^{-1} & 0 & 0\\ \frac{i\beta}{\alpha\omega}R_{\delta}^{-1}V''_{w} & 0 & 0 & 0 & 0\\ (i\alpha^{t})^{-1}V'_{w} & (3R_{\delta}^{-1} + c^{t}(i\alpha^{t})^{-1}) & 0 & -(\alpha^{t})^{-2}R_{\delta}^{-1} & 0 \end{bmatrix}.$$
 (A 14)

$$\boldsymbol{\eta}^t = \hat{\boldsymbol{\eta}}^t \exp[\mathrm{i}(\alpha^t x_1^t - \omega t)],\tag{A 15}$$

where $\hat{\boldsymbol{\eta}}^t = \boldsymbol{b} \exp(i\gamma x_3^t)$.

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$$Det[\rho\omega^2\delta_{ps} - C_{pqrs}^t k_q^t k_r^t] = 0, \tag{A 16}$$

$$\langle k_1^t, k_2^t, k_3^t \rangle = \langle \alpha^t, 0, \gamma \rangle \tag{A 17}$$

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$$f(\theta, \psi) = (g(\psi)\cos\theta, g(\psi)\sin\theta, f(\psi)). \tag{A 18}$$

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$$f(\psi_1) = \frac{3b}{\pi [2(a+b\cos\psi_1)]^{3/2}} \int_0^{2\pi} \frac{(\sin\psi_1 - \sin\psi)(a+b\cos\psi)^{1/2}}{[1-\cos(\psi_1 - \psi)](2+\alpha)^{1/2}} dx, \quad (A 19)$$

375
$$g(\psi_1) = \frac{3}{\pi [2(a+b\cos\psi_1)]^{3/2}} \int_0^{2\pi} \left(\frac{a+b\cos\psi}{2+\alpha}\right)^{1/2} \left\{ f(\psi)[(\cos\psi_1 - b\beta_1)S + \beta_1 P] \right\}$$

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$$\times \frac{\sin \psi_1 - \sin \psi}{1 - \cos(\psi_1 - \psi)} + g(\psi) \left[\left(2 + \alpha - \frac{(\sin \psi_1 - \sin \psi)^2}{1 - \cos(\psi - \psi_1)} - b^2 \gamma \right) S \right]$$

$$+\left(b^2\cos\psi_1\gamma - \frac{a}{b}\alpha\right)F(\frac{1}{2}\pi,\delta) - (2+\alpha)\cos\psi_1E(\frac{1}{2}\pi,\delta)\right]\right\}\mathrm{d}\psi,\tag{A 20}$$

380 $\alpha = \alpha(\psi, \psi_1) = \frac{b^2 [1 - \cos(\psi - \psi_1)]}{(a + b \cos \psi)(a + b \cos \psi_1)}, \quad \beta - \beta(\psi, \psi_1) = \frac{1 - \cos(\psi - \psi_1)}{a + b \cos \psi}.$ (A 21)

$$H(0) = \frac{\epsilon \overline{C}_{v}}{\tilde{v}_{T}^{1/2}(1-\beta)}, \quad H'(0) = -1 + \epsilon^{2/3}\overline{C}_{u} + \epsilon \hat{C}'_{u};$$

$$H''(0) = \frac{\epsilon u_{*}^{2}}{\tilde{v}_{T}^{1/2}u_{P}^{2}}, \quad H'(\infty) = 0.$$
(A 22)

LEMMA 1. Let f(z) be a trial Batchelor (1971, pp. 231–232) function defined on [0, 1].

Let Λ_1 denote the ground-state eigenvalue for $-d^2g/dz^2 = \Lambda g$, where g must satisfy $\pm dg/dz +$

 $\alpha g = 0$ at z = 0, 1 for some non-negative constant α . Then for any f that is not identically

385 zero we have

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$$\frac{\alpha(f^{2}(0) + f^{2}(1)) + \int_{0}^{1} \left(\frac{\mathrm{d}f}{\mathrm{d}z}\right)^{2} \mathrm{d}z}{\int_{0}^{1} f^{2} \mathrm{d}z} \geqslant \Lambda_{1} \geqslant \left(\frac{-\alpha + (\alpha^{2} + 8\pi^{2}\alpha)^{1/2}}{4\pi}\right)^{2}. \tag{A 23}$$

COROLLARY 1. Any non-zero trial function f which satisfies the boundary condition f(0) = f(1) = 0 always satisfies

$$\int_0^1 \left(\frac{\mathrm{d}f}{\mathrm{d}z}\right)^2 \mathrm{d}z. \tag{A 24}$$

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